

A novel numerical method for fluid structure interaction problems

UNIVERSITÀ **DEGLI STUDI** DI PADOVA

Federico Dalla Barba - 33rd Cycle

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FLUID-STRUCTURE INTERACTION AND HYDRAULIC FRACTURING: OVERVIEW AND MOTIVATIONS

- Fluid-Structure Interaction (FSI) problem:
 - Interaction between a fluid flow and rigid or deformable solid structures:
 - Force exchange across **sharp**, **geometrically complex and time**evolving interfaces
 - Solid mechanics and fluid dynamics governed by **different** constitutive laws
 - Hydraulic Fracturing (HF)
 - Fracture mechanics is involved
 - Crack-formation, branching and break-up in solids

due to fluid-induced stresses or fluid-driven fatigue

- Multi-physics and strongly nonlinear problem
- Analytical solution are not possible
- Models for applications have limited reliability

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• FSI and HF in aerospace engineering:

- Liquid sloshing in fuel tanks
- Aeroelastic flutter of wings
- Formation of cracks in wings and turbo-machinery components





- FSI and HF in planetary sciences:
 - Erosion processes on planetary surfaces





• FSI and HF in geotechnic: • Fracking



Norris et al. Annu. Rev. Earth Planet. Sci. 2016. 44:321–51













OBJECTIVES AND METHODOLOGY

- Objectives:
 - Development of a numerical tool capable to reproduce the physics of generic FSI problems involving solid fracture
 - Investigation of the physics of FSI with solid fracture

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Methodology:	
Peridvnamics (PD):	

- Reformulation of solid mechanics in terms of integral equations
- Crack formation, crack branching and solid fracture are intrinsically accounted for in the theory
- Incompressible Navier-Stokes equations (NS)
 - Prediction of fluid flow dynamics
 - Direct Numerical Simulation (DNS): all the scales of turbulent motions are directly solved on the computational grid without using turbulence model
- Immersed Boundary Method (IBM)
 - Imposition of no-slip and no-penetration BCs on geometrically complex interfaces
 - No need for grid update during simulation









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MOVING FLUID-SOLID INTERFACE: NOT CONFORMING TO THE EULERIAN GRID













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• Peridynamics is a reformulation of continuum mechanics based on non-local integral equations:

- A discretized peridynamic solid is a **set of finite size material particles**
- Material particles mutually interact via micro-elastic potentials that generate bond forces
- Interactions (*bonds*) vanish beyond a threshold distance, referred to as *horizon*, δ



DISCRETE BOND-BASED PERIDYNAMICS: BASIC CONCEPTS



Body discretization: cubic and finite-size particles of edge-size Δs



• Peridynamic equations:

$$\frac{dX_h}{dt} = U_h$$
$$\frac{d^2X_h}{dt^2} = \sum_{l=1}^{N_h} f_{h,l} \Delta V_l + F_{ext,h}$$

• *f* is a force density (force per unit volume square) and is referred to as *pairwise density function*:

• $f_{h,l}$ is the force per unit volume square that material point X_l exerts on X_h

• $f_{l,i} = -f_{h,l}$ is the force per unit volume square that material point X_h exerts on X_l

PROS:

- The usage of integral equations avoids the onset of singularities in the evaluation of partial derivatives that affect classical local theories when crack formation is taken into account
- Intrinsic crack management capabilities
- CONS:
 - High computational cost!







DENSITY AND BOND BREAK-UP

• The pairwise density function, $f_{h,l}$, is a function of the bond stretch, $s_{h,l}$, and of the macroscopic mechanical properties of the material:

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$$f_{h,l} = c_0 \, s_{h,l} \, \Gamma_{h,l} \, \frac{X_l - X_h}{||X_l - X_h||}$$

• The **bond stretch**, $s_{h,l}$, is the ratio between the actual relative distance in a particle pair, $|X_l - X_h|$, and the related distance in the reference configuration of the body, $|X_{0,l} - X_{0,h}|$:

$$s_{h,l} = \frac{|X_l - X_h|}{|X_{0,l} - X_{0,h}|}$$

- c_0 is the *bond micro-modulus* and is a function of the Young's modulus, *E* ,and of the horizon, δ
- The parameter $\Gamma_{h,l}$ accounts for bond break-up:

$$\Gamma_{h,l} = \begin{cases} 1, & s_{h,l} < s_0, \ \forall t \ge 0\\ 0, & otherwise \end{cases}$$



• Peridynamics - Intrinsic crack detection and crack-branching prediction capabilities:

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• A bond breaks when its stretch, *s*, overcomes a threshold value, the limit bond stretch, *s*₀ • The limit bond stretch, s_0 , is a function of the macroscopic mechanical properties of the material: the energy release rate, *G*, and the horizon, δ

Bond breakage is permanent!









- Solid surfaces are defined by means of a specific sub-set of material particles (Lagrangian markers)
- A 3D surface detection algorithm is used to check if a material particle is located on the solid surface or interior
- Principle (2D case):
 - The space surrounding each material particle, X_h , is divided into 8 circular sectors
 - Each particle, X_l , in the family of X_h is associated with only one of the sectors
 - CRITERION: a particle is located on the solid surface if 2 or more consecutive sectors are empty (90°)



 X_h is the interior



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AUTOMATIC DETECTION OF SOLID SURFACES AND



• The vectors normal to the surface can be computed at the position of each material particle located on the solid surface:

$$\boldsymbol{n}_{h} = -\frac{\sum_{l=1}^{N_{h}} (\boldsymbol{X}_{l} - \boldsymbol{X}_{h}) \Gamma_{h,l} \Delta V_{l}}{\sum_{l=1}^{N_{h}} \Gamma_{h,l} \Delta V_{l}}$$

- The basic idea is that of **volume-averaging the relative positions** of the material particles X_l in the family of X_h
- The normal unit vector is $\hat{n}_h = \frac{n_h}{|n_h|}$, the tangent, \hat{t}_h , and binormal vectors, $\hat{\boldsymbol{b}}_h$, follow immediately



Normals computed on the surface of a peridynamic-discretized sphere





- The dynamics of fluid flows is described by employing the incompressible Navier-Stokes equations that are solved on a fixed, uniform and equispaced Eulerian grid:
- All the length-scales of the turbulent motion are directly resolved on the grid without using turbulent model: Direct Numerical Simulation (DNS)

$$\nabla \cdot \boldsymbol{u} = 0$$

$$\rho_f \left(\frac{\partial \boldsymbol{u}}{\partial t} + \boldsymbol{u} \cdot \nabla \boldsymbol{u} \right) = -\nabla p + \mu_f \nabla^2 \boldsymbol{u} + \rho_f \boldsymbol{F}_{IBM}$$

BCs are directly imposed by means of ghost nodes at the limit boundaries of the computational domain

PROBLEM: BCs have to be imposed to the flow on the solid-liquid interface, but the Eulerian grid nodes do not coincide with the moving solid surface. BCs cannot be directly imposed on the grid nodes e.g. $u_{i,i,k} = 0$!

Immersed Boundary Method (IBM): a fictitious force field, F_{IBM} , distributed on the grid nodes near the solid-fluid interface, is used to indirectly impose BCs!



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• IBM PROS:



- The eulerian grid can be non-conforming to the solid surface!
- Grid update is not necessary during the simulation to preserve the match of grid nodes with solid surfaces!
- BCs can be easily and efficiently applied to geometrically complex interfaces!









- **PROBLEM:** boundary conditions have to be imposed to the flow on the moving solid-liquid interface:
 - on no-slip boundary condition
 - on no-penetration boundary condition
- The force field can be computed by using an iterative procedure (**multi-direct forcing scheme**) until convergence of the force field:





• IBMs employ a fictitious force field applied to the fluid flow such that, near the interface, the fluid is forced to move with the same local velocity of the solid body

(2) Computation of the forcing

(3) Spreading of the forcing on the fluid grid

$$= \frac{U_h - U_f(X_h)}{\Delta t}$$

• U_h is the actual velocity of the material particle X_h • $U_f(X_h)$ is the fluid velocity field interpolated at the actual position of the centroid of the material particle X_h









• The forces exerted by the liquid flow on the solid are computed by employing the *normal probe method.* For any material particles located on the solid surface:

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- 1. A probe of length $l_p = 2\Delta x$ starting from X_h is sent into the fluid along the direction defined by the local normal unity vector to the surface, \hat{n}
- **Interpolation of the flow velocity field** at the probe tip (point **T**, see the stencil 2. on the right) by tri-linear interpolation
- **Interpolation of flow pressure and pressure gradient** at the probe tip (point **T**, 3. see the stencil on the right) by tri-linear interpolation (to compute $p|_{X_{\mu}}$)
- 4. Computation of the shear and normal stresses, τ_{ξ} , τ_{η} , τ_{ζ} , at the probe root (position X_h) in the local coordinate system, (ξ, η, ζ)
- **Change of reference frame.** Stresses transformation from local frame, (ξ, η, ζ) , to 5. global coordinate system, (x, y, z): $\tau_{\xi}, \tau_{\eta}, \tau_{\zeta} \rightarrow \tau_{x}, \tau_{y}, \tau_{z}$

$$\begin{aligned} \tau_{\xi} &= \mu_{f} \frac{\partial u_{\xi}}{\partial \eta} \bigg|_{X_{h}} & \frac{\partial u_{\xi}}{\partial \eta} \bigg|_{X_{h}} &= \frac{(U_{f}(X_{T}) - U_{h}) \cdot \hat{t}}{l_{p}} \\ \tau_{\eta} &= \mu_{f} \frac{\partial u_{\eta}}{\partial \eta} \bigg|_{X_{h}} - p \bigg|_{X_{h}} & \frac{\partial u_{\eta}}{\partial \eta} \bigg|_{X_{h}} &= \frac{(U_{f}(X_{T}) - U_{h}) \cdot \hat{n}}{l_{p}} & U_{f}(X_{T}) \\ \tau_{\zeta} &= \mu_{f} \frac{\partial u_{\zeta}}{\partial \eta} \bigg|_{X_{h}} & \frac{\partial u_{\zeta}}{\partial \eta} \bigg|_{X_{h}} &= \frac{(U_{f}(X_{T}) - U_{h}) \cdot \hat{b}}{l_{p}} \end{aligned}$$

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COMPUTATION OF FLUID DYNAMIC FORCES



 T_T) fluid velocity filed polated at the probe tip, T



 Δx : Eulerian grid spacing



2D schematic of the interpolation stencil used to compute shear and normal stresses in the local frame of reference

- A local frame of references centered at X_h is defined:
 - ξ along local tangent vector, \hat{t}
 - η along local normal vector, \hat{n}
 - $\hat{\boldsymbol{\zeta}}$ along local bi-normal vector, $\hat{\boldsymbol{b}}$











• The procedure has been implemented to obtain a numerical code to address FSI problems considering crack formation, crack branching and fracture:

- FLUID SOLVER (developed upon open-source CaNS by Pedro Costa):
 - Second order **finite difference schemes** for space discretization
 - Third order, low storage **Runge-Kutta** time marching algorithm
 - **Pressure correction** algorithm
- PERIDYNAMIC SOLVER:
 - **Fully explicit** algorithm
 - Third order, low storage **Runge-Kutta** time marching algorithm
- IBM:
 - Multi-direct forcing scheme (3 steps)

• PARALLELIZATION:

- MPI-based parallel structure. The code can be run on both shared and distribute memory systems (tested up to 1024 cores)
- Excellent scaling performances

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• 2D rectangular and linear elastic solid in a laminar



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- Validation by comparison:
 - The temporal evolution of the position of the solid centroid is chosen as target
 - Two different peridynamic discretization are considered to asses grid convergence (D1
 - The results predicted using the present numerical tool are compared with the results obtained using a commercial software COMSOL MULTIPHYSICS
 - Testing and validation campaign:
 - Many validation benchmarks to validate the methodology:
 - Crack detection and propagation
 - Computation of fluid forces
 - IBM
 - Methodology and related validation in: Dalla Barba F., Picano F. (2020). A novel approach for direct numerical simulation of hydraulic fracture problems. Flow, Turbulence and Combustion, Vol. 105, p. 335-357, ISSN: 1386-6184, doi: 10.1007/s10494-020-00145-x.

• Problem description:

- An incompressible, fully-turbulent stream flows through a rectangular-cross-section channel
- The channel is **periodic along the flow and span-wise directions**

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- The upper and lower walls of the channel are rigid and impermeable
- A solid layer with linear-elastic and brittle mechanical properties is attached to the lower wall of **the channel** (the lower wall acts as a rigid and impermeable substrate)
- Relevance: the problem is of relevant interest in environmental and planetary sciences (e.g. erosion processes, geomorphology, etc.) as well as in aerospace field (e.g. erosion due to intensive turbulent flows in contact with ablative material, nozzle throat erosion in rocket engine, etc.)

• Mechanical properties (non-dimensional):

Bulk Reynolds number:	$Re_b = U_b h / \nu_f = 4500$
Friction Reynolds number:	$Re_{\tau} = u_{\tau}h/\nu_f = 147.5$
Young's modulus:	$E/(\rho_f U_b^2) = 2.0 \cdot 10^{-1}$
Poisson ratio:	$\nu_{s} = 0.25$
Density ratio:	$\rho_s/\rho_f = 5$
• Fracture energy release rate:	$G_0/(Eh) = 2.6 \cdot 10^{-5}$

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APP. #1: NUMERICAL STUDY OF THE EROSION OF A BRITTLE SUBSTRATE IN A TURBULENT CHANNEL FLOW

Rectangular computational domain for the Eulerian phase:

- Periodic BCs along the flow and span-wise directions
- No-slip and no-penetration BCs on the upper and lower boundaries of the domain
- Eulerian grid: $N_x \times N_y \times N_z = 288 \times 144 \times 108$ nodes

Peridynamic representation of the brittle, erodible substrate by cubic partitioning:

- Solid substrate attached to the impermeable and rigid lower wall of the channel
- Cubic particles on a Cartesian grid in the reference configuration: $N_x \times N_y \times N_z = 288 \times 144 \times 14$

Initialization:	Fluid region (white)		
Fully-developed turbulent flow	Duittle cubet		
Statistically-stationary equilibrium	(light grey)		
configuration for the deformation of			
the colid substrate	Fixed constraint (1		
the sond substrate	three layer of parts		
	(dark grey)		

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EROSION

 $0.00 \quad 0.20 \quad 0.40' \ 0.60 \quad 0.80 \quad 1.00$

• Damage accumulates over time until break-up occurs

 $t/\tilde{t} = 16.75$

Coherent structures of the flow by Q-criterion (Q = 1)

Damage level, Φ

Axial velocity of the flow, u

 $t/\tilde{t} = 25.50$

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• Erosion by fluid-drive fatigue mechanism:

- Turbulent fluctuations can locally (and randomly) increase the **intensity of wall**
 - stresses up to the ultimate strength of the brittle substrate
- Local damages are produced and cracks form
- Cracks reduce the local strength of the substrate
- Lower intensity hydrodynamic stresses can produce a damage

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STREAMBED

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1.5 y/h

• Volumetric erosion rate:

• Volume of eroded material:

$$e(t) = \frac{d}{dt} \left(\frac{V(t) - V(0)}{V(0)} \right)$$

$$E(t) = \int_0^t e(\hat{t}) d\hat{t}$$

• Rate of erosion:

• The volumetric erosion rate increases linearly in time

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- The total volume of eroded material grows quadratically
- The erosion process accelerates!

APP. #1: EROSION RATE: THE PROCESS ACCELERATES

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- Peaks on the stream-bed act locally as obstacles for the flow stream
- Small-scale and high-intensity vortexes originate over the peaks
- This small-scale vortexes enhance the intensity of local wall-stresses up to 20 times the mean hydrodynamic stress
- Peaks break-up and the scoured regions expand in the downstream direction of the flow
- The vortexes move downstream, stationing over the new peaks and sustaining the process
- As the surface becomes more irregular, the number and intensity of small-scale coherent structures increases, enhancing the erosion rate and wall stresses
- The erosion process globally accelerates!

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APP. #1: WHY EROSION ACCELERATES? STRESS ENHANCEMENT BY TURBULENCE-WALL INTERACTION

APP. #1: WHY EROSION ACCELERATES? PROBABILITY DENSITY FUNCTION OF WALL STRESSES

 $t/\tilde{t} = 16.75$

 $t/\tilde{t} = 25.5$

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- The occurrence of high-intensity turbulent structures near the wall increases in time due to the scouring of the stream-bed.
- High-intensity turbulent events enhance the local wall stresses.
- The PDFs of the wall stresses, τ_{zx} , τ_{zy} , $\tau_{zz'}$, widesout.

- By comparing the cumulative distribution function of the shear stress, $\tau_s = \sqrt{\tau_{zx}^2 + \tau_{zy}^2}$, with the ultimate strength of the material it results that:
 - At the beginning of the process the number of turbulent events leading to a break-up are only 9% of the overall turbulent events.
 - At the end of the process the number of turbulent events leading to a break-up increases up to 12.5% of the overall turbulent events!
- The irregular shape of the stream-bed promotes the formation of coherent, high-intensity turbulent structures. The latter, enhance at their turn the wall-stresses, promoting the break-up and the formation of more irregularities on the stream-bed.

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APP. #1: WHY EROSION ACCELERATES? CUMULATIVE DENSITY FUNCTION OF WALL STRESSES

Results and discussion 0 submitted to Journal of Fluid Mechanics (under consideration): Dalla Barba F., Picano F. (2020). Direct numerical simulation of the scouring of a brittle stream-bed in a turbulent channel flow

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• WORK IN PROGRESS

- 0.050
- 0.040
- 0.030 ~
- 0.020 <u>E</u>
- 0.010
- 0.000

- DNS of homogeneous isotropic turbulence: solid grains of linear elastic and brittle materials are dispersed in the flow
- Study of the mechanism leading to **fluid-driven-fatigue** break-up of the grains
- The problem is of relevant interest for environmental, geotechnical and industrial applications:
 - Fragmentation of micro plastics in oceans and sees
 - Flock disruption in multiphase flow

MEDIA IN LAMINAR FLOWS

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• WORK IN PROGRESS

- DNS of laminar flow through a porous media
- Study of the mechanism leading to the **break-up of a** porous solid in laminar flow
- The problem is of relevant interest for environmental, geotechnical and industrial applications:
 - Fragmentation of rocks and rock aggregates in fault systems
 - Degradation of porous electrodes in fuel cells and flow batteries

- FSI problems with crack formation and solid media fracture can be treated numerically in a Navier Stokes - peridynamics - IBM framework
- A massive parallel numerical tool capable to address general FSI problems accounting for crack formation and fracture in solids has been developed
- Validation and testing have been performed obtaining promising results:
 - Capability of the solver to reproduce solid media fracture and crack branching due to fluid-induced forces
 - Capability of IBM to impose **no-slip and no-penetration boundary** conditions on complex and time evolving interfaces
 - Accurate computation of fluid forces on solid via normal probe method
 - Automatic detection of cracks and new interfaces

FINAL REMARKS AND OUTCOMES OF THE RESEARCH

- The method and the new numerical equipment have been employed to address the simulation of the erosion and break up of brittle substrate in turbulent flows:
 - The basic mechanisms governing the process have been identified and characterized
 - The outcomes of the research and future development may be relevant in:
 - Environmental and planetary science applications, e.g. erosion processes on planetary surfaces
 - Aerospace applications, e.g. accurate control of the erosion of nozzle throat in rocket engines

• PUBBLICATIONS

- Ph.D. related publications:
 - Dalla Barba F., Picano F. (2020). A novel approach for direct numerical simulation of hydraulic fracture problems. Flow, Turbulence and Combustion, Vol. 105, p. 335-357, ISSN: 1386-6184, doi: 10.1007/ s10494-020-00145-x.
 - Dalla Barba F., Picano F. (2020). A new method for fully resolved simulations of fracturing in fluidstructure interaction problems. In: ERCOFTAC Series. ERCOFTAC SERIES, Vol. 27, p. 469-475, Springer, ISBN: 978-3-030-42821-1, ISSN: 1382-4309, doi: 10.1007/978-3-030-42822-8_62.
 - Dalla Barba F., Campagnari P., Zaccariotto M., Galvanetto U., Picano F. (2020). A fluid-structure interaction model based on peridynamics and Navier-Stokes equations for hydraulic fracture problems. In: Proceedings of the 6th European Conference on Computational Mechanics: Solids, Structures and Coupled Problems, ECCM 2018 and 7th European Conference on Computational Fluid Dynamics, ECFD 2018. p. 89-100, International Centre for Numerical Methods in Engineering, CIMNE, Scottish Events Campus, gbr, 2018.

• Other publications produced during the Ph.D. course:

- *Ciottoli P.P., Battista F., Malpica Galassi R., Dalla Barba F., Picano F. (2020). Direct numerical simulations of the* evaporation of dilute sprays in turbulent swirling jets. Flow, Turbulence and Combustion, 1-23, ISSN: 1386-6184, doi: 10.1007/s10494-020-00200-7.
- Dalla Barba, F., Picano, F. (2019). Evaporation dynamics in dilute turbulent jet sprays. In: ERCOFTAC Series. ERCOFTAC SERIES, Vol. 25, p. 221-227, Springer, ISBN: 978-3-030-04914-0, ISSN: 1382-4309, doi: 10.1007/978-3-030-04915-7_30.
- Dalla Barba F., Picano F. (2018). Clustering and entrainment effects on the evaporation of dilute droplets in a turbulent jet. Physical Review Fluids, Vol. 3, 034304, ISSN: 2469-990X, doi: 10.1103/PhysRevFluids.3.034304

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PUBLICATIONS AND TRAINING ACTIVITIES

ISAS	
СОГОМВО	

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PERSONAL TRAINING PLAN OF DOCTORAL STUDENT FEDERICO DALLA BARBA

DUCATIONAL ACTIVITIES ACTIVATED BY THE STMS	PHD COURSE						
nterdisciplinary Module/Activity		Lecturer	Expected credits	Frequency (YES/NO)	Exam (YES/NO)*	Date of exam	Attained credits
xploring the solar system and its environment		Prof. Marzari / Pajola/ Lucchetti	4	YES	YES	17/05/2018	4
undamentals of measurements and PC-based applications		Prof. Pertile / Rossi	4	YES	YES	11/07/2018	4
Mechanical and thermal properties of material for aerospace		Prof. Galvanetto / Zaccariotto	4	YES	YES*	14/03/2019	4
Preparation of a research proposal		Prof Naletto	2	YES	YES	19/06/2020	2
Curriculum oriented seminars		Lecturer	Expected credits	Frequency (YFS/NO)	Exam	Date of exam	Attained credits
Mechanics of vehicle		Prof. Franceschini	0.4	YES	YES	20/02/2018	0.4
The radiation environment in space: evaluating dose, material		Prof. Rando	0.4	YES	YES	28/02/2018	0.4
Analysis of complex dynamics using chaos indicat	fors	Prof Guzzo	0.4	VES	VES	29/03/2018	0.4
Indivision of complex dynamics using chaos maled	vironment	Prof. Corso	0.4	VES	VES	18/06/2018	0.4
Advanced Computational Modeling of Solid/Eluio	Interactions	Prof Picano	0.4	VES	VES	19/06/2018	0.4
Catellite Navigation and attitude control using G	VSS	Prof. Caporali	0.4	VES	VES	23/01/2019	0.4
Space instrument testing with stratospheric hallo	ons and drones	Prof. Bettanini	0.4	VES	VES	06/02/2019	0.4
Jigh efficiency EUV ontics for solar physics applic	ation	Prof. Corso	0.4	VES	VES	08/02/2019	0.4
ingle efficiency 200 optics for solar physics applic	ation	Prof. Pernechele	0.4	VES	VES	16/04/2019	0.4
inite Element Analysis of multi-phase porous me	dia with		0.4	TLS	TLJ	10/04/2019	0.4
nite Element Analysis of multi-phase porous media, with particular attention to strain localization and desiccation cracks		Prof. Sanavia	0.4	YES	YES	20/02/2010	0.4
Iy low cost experiments in Earth atmosphere and	d stratosphere:	Prof. Bettanini	0.08	YES	NO	-	0.08
DTHER EDUCATIONAL ACTIVITIES			Exported	Fraguanay	Evam		Attained
itle of the activity (Date/Period/University)	Lecturer	Duration of activity	credits	(YES/NO)	(YES/NO)	Date of exam	credits
Course: Finite Elements Method	Prof. Gambolati	32 h	6.4	YES	YES	10/07/2019	6.4
Course: Reactive Fluid Mechanics	Prof. Canu	12 h	0.48	YES	NO	-	0.48
	•						
Congress: ECCM-ECFD, 11-12/06/18, Glasgow		15 h (36x20 min talks + 2x90min plenary lectures)	0.6	YES	-	-	0.6
Congress: Euromech 596, 09-10/05/18, Venice	-	12 h (40x15min talks + 2x60 min plenary lectures)	0.48	YES	-	-	0.48
Didattica integrativa: Aerodinamica II, Laurea Aagistrale Ingegneria Aerospaziale, primo emestre 2017/2018	-	30 h	2.4	-	-	-	2.4
Didattica integrativa: <i>Meccanica dei fluidi, aurea in Ingegneria dell'Energia,</i> secondo emestre 2017/2018	-	10 h	0.8	-	-	-	0.8
Didattica integrativa: Aerodinamica, Laurea in ngegneria Aerospaziale, primo semestre 2018/2019	-	10 h	0.8	-	-	-	0.8
Didattica integrativa: Aerodinamica II, Laurea Magistrale in Ingegneria Aerospaziale, secondo emestre 2018/2019		20 h	1.6	-	-	-	1.6
Didattica integrativa: Aerodinamica, Laurea in ngegneria Aerospaziale, primo semestre 2019/2020	-	20h	1.6	-	-	-	1.6
Didattica integrativa: Aerodinamica 2, Laurea Magistrale in Ingegneria Aerospaziale, secondo emestre 2019/2020		10h	0.8				0.8
Didattica integrativa: Laboratorio di Iuidodinamica computazionale, Laurea Magistrale in Ingegneria Aerospaziale, secondo remestre 2019/2020		10h	0.8				0.8
otal of expected ECTS credits attainable in edu	cational activities	s (>30):	34.84	Total of crec educational 29/10/2020	lits attaine activities (a)	d in at date	34.84

⁵ Specify which exam will be done as an academic lecture

Thank you for your attention