Morphological and compositional analysis of boulder distribution on comet 67P/Churyumov-Gerasimenko

PhD student Pamela Cambianica

Admission to Third Year 13 September 2018

Supervisor: Giampiero Naletto Co-supervisor: Gabriele Cremonese







Credits: ESA

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• To define a method to analyze in a quantitative manner populations of boulders





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- To link the method with others described in literature





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- To define possible processes responsible for the boulder fragmentation through OSIRIS image analysis



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- To understand the rule of thermal stress and fatigue in terms of propagation of cracks and fragmentation



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Credits: ESA

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- To link the method with others described in literature
- To define possible processes responsible for the boulder fragmentation through OSIRIS image analysis
- To understand the rule of thermal stress and fatigue in terms of propagation of cracks and fragmentation
- To develope a fragmentation model able to explain the presence of some features, like boulders, on the surface of comet 67P/C-G



The Rosetta mission – OSIRIS instrument









Analysis of OSIRIS images

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Selection of surface images – Pre and post-perihelion



Imhotep

NAC_2014-09-29T13.29.30.598Z_ID30_1397549600_F22

NAC_2016-07-09T11.25.15.786Z_ID30_1397549000_F41



NAC_2014-12-10T06.29.11.447Z_ID10_1397549002_F24

NAC_2016-07-20T08.02.48.392Z_ID30_1397549001_F22.

Hatmehit

NAC_2014-12-12T17.42.03.690Z_ID30_1397549500_F24

NAC_2016-07-23T17.54.43.732Z_ID30_1397549002_F41



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Imhotep

NAC_2014-09-29T13.29.30.598Z_ID30_1397549600_F22 NAC_2016-07-09T11.25.15.786Z_ID30_1397549000_F41

<u>Hapi</u>

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NAC_2014-12-12T17.42.03.690Z_ID30	_1397549500_F24
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Cumulative size-frequency distribution

Understanding the SFD of rocks on surfaces can supply geological information related to the body's origin and evolution



A power function can be used to fit data from every regions to represent the general form of rock size distribution

$$N(\geq a) = ka^{-D}$$



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Cumulative size-frequency distribution – Fractal theory

Understanding the SFD of rocks on surfaces can supply geological information related to the body's origin and evolution



Empirical data have suggested that the size distribution of material expected from fractures and fragmentation would allow a fractal rule

$$N\left(\frac{1}{b_i}\right) = k\left(\frac{1}{b_i}\right)^{-r}$$
 (Mandelbrot, 1982)
$$N(\geq a) = ka^{-D}$$

k number of initiators of unit lengthb scaling factor > 1r fractal dimension

The SFD curve can be represented by a fractal theory, a power-law which appears as a straight line in a log-log plot



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Analysis of a complex 2D pattern by breaking an image into smaller pieces, and analyzing the pieces at each smaller scale

- How many boxes are required to cover the image?
- Calculation of the Minkowski-Bouligand dimension seeing how this number changes as the grid became finer





Fractal theory – BoxCount (2/2)



The discrepancy between the two curves indicates a possible fractal behavior of the image

n(r) = number of boxes needed to cover the set as a function of the size r of the boxes Solid line = power-law $N(r)=N_o r^{-Df}$. It should appear if the set is fractal Dotted line = it appears showing the scaling $N(r)=r^2$ for comparison, expected for a space-filling 2D image



Cumulative fractional area

- The CFA covered by rocks *vs* diameter curve is represented in a log-log plot.
- Usually, the distribution is fitted by an exponential or power-law equation



$$F(\geq D) = Kx^{-q(D)}$$

F(D) is the CFA covered by rocks of diameter D or larger
k is the total area covered by all rocks
q(x) governs how abruptly the area covered by rocks decreases with increasing diameter



Boulders shape

The morphologies of rocks should provide records on rock surface processes if signature in their shape and surface texture can be identified and interpreted.

- Sphericity and elongation reflect the lithology of the mass itself
- Roundness describes transport or weathering history

The final shape is strongly influenced by the composition of particles

- Slate rocks tend to split into planar fragments
- Jointed rocks tend to split into cubic fragments
- Corners and edges are most vulnerable than faces

Shape factors

Dimensionless quantities calculated from measured dimension, such as diameter, area, perimeter, etc. The factors are normalized, that is the values range from 0-1 where 1 represents an ideal case of maximum symmetry.

Aspect Ratio Circularity Roundness Compactness Elongation Solidity Convexity Feret's diameter



Boulders shape – Source of errors

- To classify each area in terms of shape factors
- To compare pre and post perihelion shape factors

Viewpoint

Elevation

Azimuth

Center of

Plot Box

(A) Random

Elongation and azimuth

Synthetic image test





Quantitative analysis of Imhotep, Hapi and Hatmehit boulder populations on comet 67P/Churyumov-Gerasimenko

P. Cambianica¹, G. Cremonese², G. Naletto^{5, 1, 6}, A. Lucchetti², M. Pajola², L. Penasa¹, E. Simioni², M. Massironi^{4, 1}, S. Ferrari¹, F. LaForgia³, H. Sierks⁷, P. L. Lamy⁸, R. Rodrigo^{9, 10}, D. Koschny¹¹, B. Davidsson¹², M. A. Barucci¹³, J.-L. Bertaux¹⁴, I. Bertini³, D. Bodewits¹⁵, V. Da Deppo⁶, S. Debei¹⁶, M. De Cecco¹⁷, J. Deller⁷, S. Fornasier¹³, M. Fulle¹⁸, O. Groussin¹⁹, P. J. Gutiérrez²⁰, C. Güttler⁷, S. F. Hviid²¹, W.-H. Ip^{22, 23}, L. Jorda¹⁹, H. U. Keller^{24, 21}, J. Knollenberg²¹, E. Kührt²¹, M. Küppers²⁵, L. M. Lara²⁰, M. Lazzarin³, J. J. López-Moreno²⁰, F. Marzari⁵, X. Shi⁷, N. Thomas^{26, 27}, C. Tubiana⁷, and J.-B. Vincent²¹

(Affiliations can be found after the references)







Analysis of OSIRIS images

- Quantitative analysis of Imhotep, Hapi and Hatmehit boulder populations on comet 67P/Churyumov- Gerasimenko
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Measurements of erosion and dust deposits in the Hapi region





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Dust cover or poor spatial resolution?

Height of boulders through and the lengths of shadows can improve the knowledge of the erosion and deposit variation of the dust on the comet surface









Matlab tool – Selection of an epoch

- We defined the boresight and the frame of instrument (NAC) by spice kernels
- We computed the boresight intercept of the projective ray of each pixel on the body shape (M0004 Vertices) at specific epoch.





Matlab tool – Image alignment

- Define transformation (Bundle Adjustment) between the 3D model and the pinhole camera model (it describes the mathematical relationship between the coordinates of a point in three-dimensional space and its projection onto the image plane of an *ideal* pinhole camera).
- We applied a Laplacian filter to the height model in the camera frame to fixed tie points. The Laplacian of an image highlights regions of rapid intensity change and is therefore often used for edge detection.





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Matlab tool – Local surface definition

Define surfaces around the boulders to define the mean surface reference system on which calculate the incidence angle

- To avoid the local granularity of the mesh
- To mediate the surface irregularities





Matlab tool – Incidence and emission angles

Incidence and emission angles are measured on the local surface avoiding the local granularity of the mesh.





Range from spacecraft to intercept point (km): 20.365

Intercept solar incidence angle (deg): 50.644176 Intercept emission angle (deg): 41.261912



Matlab tool – Selection of shadow's peak





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Matlab tool – Shadow's direction and length measurment







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Preliminary results

- Tool capable of measuring heights of a target on 2-d images
- Estimate of the deposit thickness within the considered region



We assume a variation not considering the erosion and activity of the boulder itself

> **T** Fragmentation model







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Thermal analysis of boulders on comet 67P/C-G



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- Evidences fo thermal fragmentation
- Far from landslides and niches

Good candidate for thermal cracking



Thermal analysis of boulders on comet 67P/C-G - Aim

Perform theoretical studies of transient temperature and thermal stress on boulder of comet 67P

COMSOL Multiphysics Modeling Software – Finite Element Method (**FEM**)



Thermal analysis of boulders on comet 67P/C-G - FEM

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Geometry and mesh (1/3) - Geometry





Geometry and mesh (2/3) - Approximations

<u>1° approximation</u> Shape of boulder: sphere 2° approximation 1⁄2 D just to compare results <u>3° approximation</u> No single point of contact















Sphere diameter (D): 40 m (Cambianica et al., in prep.) Regolith depth: 0.1<m<2.0 (Mottola et al., 2015) Block size: 2D x 2D x 2D (Molaro et al., 2015)

Mesh: Tetrahedral elements Controlled by physics + manually adjustment





Thermal analysis of boulders on comet 67P/C-G - FEM

Perform theoretical studies of transient temperature and thermal stress on boulder of comet 67P

COMSOL Multiphysics Modeling Software – Finite Element Method (FEM)





Material selection and properties



Material selection (1/8) - VIRTIS

VIRTIS

Visible InfraRed Thermal Imaging Spectrometer (Capaccioni et al., 2015)

67P composition

(Quirico et al., 2015)

- CH chemical groups
- OH chemical groups
- Refractory material
- Polyaromatic organics solid
- Sulfides
- Fe-Ni alloys



Credits: INAF-IAPS



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Material selection (3/8) – Thermal conductivity of mixtures



Cheng and Vachon model, 1968

K_c > *K_d*

Two-phase mixture

$$R_{e} = \frac{2}{\sqrt{-C(K_{d} - K_{c})[K_{c} + B(K_{d} - K_{c})]}} \\ tan^{-1}\frac{B}{2}\sqrt{\frac{-C(K_{d} - K_{c})}{K_{c} + B(K_{d} - K_{c})}} \\ + \frac{1 - B}{K_{c}}$$

•
$$K_c < K_a$$

$$\begin{aligned} R_{e} = & \frac{1}{\sqrt{-C(K_{d}-K_{c})[K_{c}+B(K_{d}-K_{c})]}} \\ & ln \frac{\sqrt{K_{c}+B(K_{d}-K_{c})}+\frac{B}{2}\sqrt{C(K_{d}-K_{c})}}{\sqrt{K_{c}+B(K_{d}-K_{c})}-\frac{B}{2}\sqrt{C(K_{d}-K_{c})}} \\ & + \frac{1-B}{K_{c}} \end{aligned}$$

Kd= thermal conductivity of the discontinuous phase **Kc**= thermal conductivity of the continuous phase

$$B=\sqrt{3Pd/2}$$

$$C = -4\sqrt{\left(\frac{2}{3}\right)Pd}$$

Pd Phase volume fraction



Material selection (4/8) – Thermal conductivity of mixtures



Three-phase mixture

$$R_e = \int \frac{dx}{K_c + (K_{d1} - K_c)y_1 + (K_{d2} - K_c)y_2}$$

- $\frac{Kd1}{Kc} > 100 \text{ and } \frac{Kd2}{Kc} > 100$
- $\frac{Kd1}{Kc} > 100 \text{ and } 10 < \frac{Kd2}{Kc} < 100$
- $10 < \frac{Kd1}{Kc} < 100 \text{ and } 10 < \frac{Kd2}{Kc} < 100$
- $\frac{Kd1}{Kc} \sim 10 \text{ and } \frac{Kd2}{Kc} \sim 10$
- $\frac{Kd1}{Kc} \sim 10 \text{ and } \frac{Kd2}{Kc} \sim 1$
- $\frac{Kd1}{Kc} \sim 1$ and $\frac{Kd2}{Kc} \sim 1$
- $\frac{Kd1}{Kc} < 1$ and $or \frac{Kd2}{Kc} < 1$



Material selection (5/8) – Thermal conductivity – Model 1





Material selection (7/8) – Thermal conductivity – Model 2





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Perform theoretical studies of transient temperature and thermal stress on boulder of comet 67P

COMSOL Multiphysics Modeling Software – Finite Element Method (**FEM**)





Material selection and properties





Physics, boundary conditions and heat source (1/3)



Physics, boundary conditions and heat source (2/3)

Physics, boundary conditions and heat source (3/3)

Heat transfer with surface-to-surface radiation

Model heat transfer by conduction, convection, and radiation

- Heat equation $\rho C_p \frac{\delta T}{\delta t} + \rho C_p \boldsymbol{u} \nabla T + \nabla \boldsymbol{q} = \mathbf{Q}$
- Fourier's law of heat conduction
 q = -k∇T

 ρ = density [kg/m³]

C_p = heat capacity at constant pressure [J/kgK]

K = solid thermal conductivity [W/mK]

u = velocity field if the parts of the model is moving Q = heat source [W/m³]

Solid Mechanics

Linear elastic material

$$\nabla S + F_{v} = 0$$

S = stress gradient Fv = external force

Measurements of erosion and dust deposits in the Hapi region

- Extend the statistics by analizing other images
- Discriminate between dust cover variation and boulder's activity
- Apply this method to other regions and other objects
- Analyze possible volumetric variations of big boulders

Thermal and stress analysis

- Shape of boulder: different shapes, irregularities, edges, cavities
- Perform the analysis form different combinations of materials, geometry, etc...
- Correlate the Von Mises stress with the propagation of cracks

• Propagate cracks

Personal training plan and Gannt bar chart

	Expected ECTS	Attained ECTS
Interdisciplinary Module/Activity	19.2	19.2
Curriculum oriented activities	17.84	11.82
Other educational activities	4.8	4.8
тот	41.84	35.52

LEVEL	ACTIVITY DESCRIPTION AND EVENTS	I YEAR	II YEAR	III YEAR
Event	Presentation for approval research	\$		
WP100	OSIRIS and the Rosetta Mission			
WP110	Study of the related literature			
WP111	The ROSETTA mission			
WP112	The OSIRIS camera			
WP200	Comets and the 67P/Churyumov-			
	Gerasimenko comet			
WP210	Study of the related literature			
WP211	Formation and evolution			
WP212	Geomorphology			
WP213	Thermodynamics			
WP300	Image analysis			
WP310	Study of the related literature			
WP320	OSIRIS archive and images			
WP330	Statistical analysis - size-frequency			
WP340	Fractal theory			
WP350	Shape factors			
WP360	Boulders and fragments shape			
Event	Admission to second year		\$	
WP400	Thermodynamic and sublimation			
WP410	Study of the related literature			
WP420	Thermal model			
WP430	Thermo-mechanical processes			
WP440	Study of ices			
WP450	Sublimation model			
Event	Admission to third year			\diamond
WP500	Modeling and use of MATLAB			
WP600	Finite Element Method			
Event	Admission to final examination			Ę
WP700	Writing thesis and reports			

Publications

Papers

- Quantitative analysis of Imhotep, Hapi and Hatmehit boulder populations on comet 67P/Churyumov- Gerasimenko Cambianica, P. et al. (in prep)
- The backscattering enhancement of comet 67P/Churyumov-Gerasimenko dust coma as seen by OSIRIS onboard Rosetta" Bertini, I. et al. 2018
- The big lobe of 67P/Churyumov-Gerasimenko comet: morphological and spectrophotometric evidences of layering as from OSIRIS data Ferrasi, S. et al. 2018
- Multidisciplinary analysis of the Hapi region located on Comet 67P/Churyumov-Gerasimenko Pajola, M. et al. 2018 (in press)

Abstracts, conference proceedings

- EPSC 2018 Thermal analysis of boulders on the 67P/Churyumov-Gerasimenko comet Cambianica, P. et al.
- SAIT 2018 Quantitative analysis of Imhotep, Hapi and Hatmehit boulder populations on comet 67P/Churyumov- Gerasimenko Cambianica, P. et al.
- EPSC 2018 Geomorphological units of Khepry and Imhotep regions of comet 67P/Churyumov-Gerasimenko Ferrari, S. et al.
- EPSC 2018 3DPD application to the first CaSSIS DTMs Simioni, E. et al.

Thanks for the attention

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