

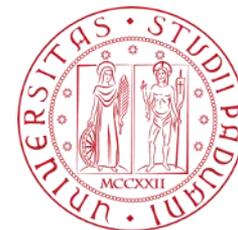
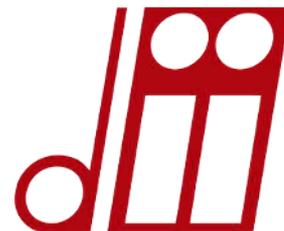
# Modeling a New Concept of Tether Deployer with Retrievable Capability for Space Applications

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Gilberto Grassi\*, Riccardo Mantellato§

\* MSc Aerospace Engineering

§ Department of Industrial Engineering  
University of Padova



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- 1. Introduction**
- 2. Proposed concept**
- 3. Models & control**
- 4. Simulations**
- 5. Conclusions**

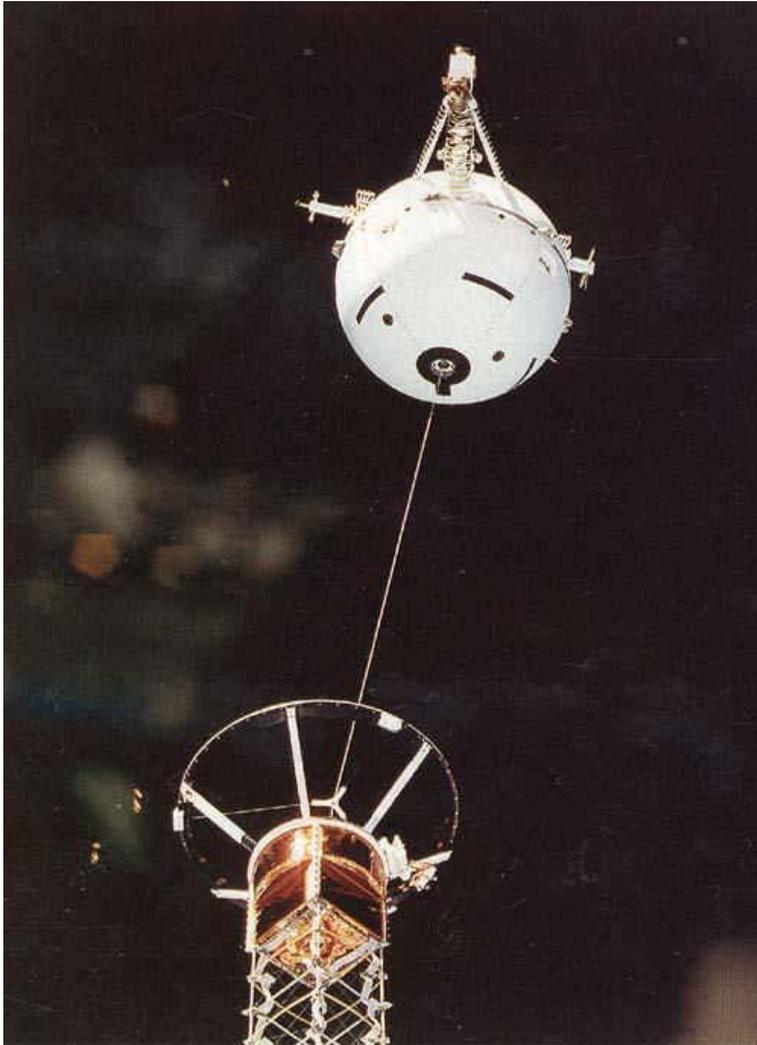


# Introduction

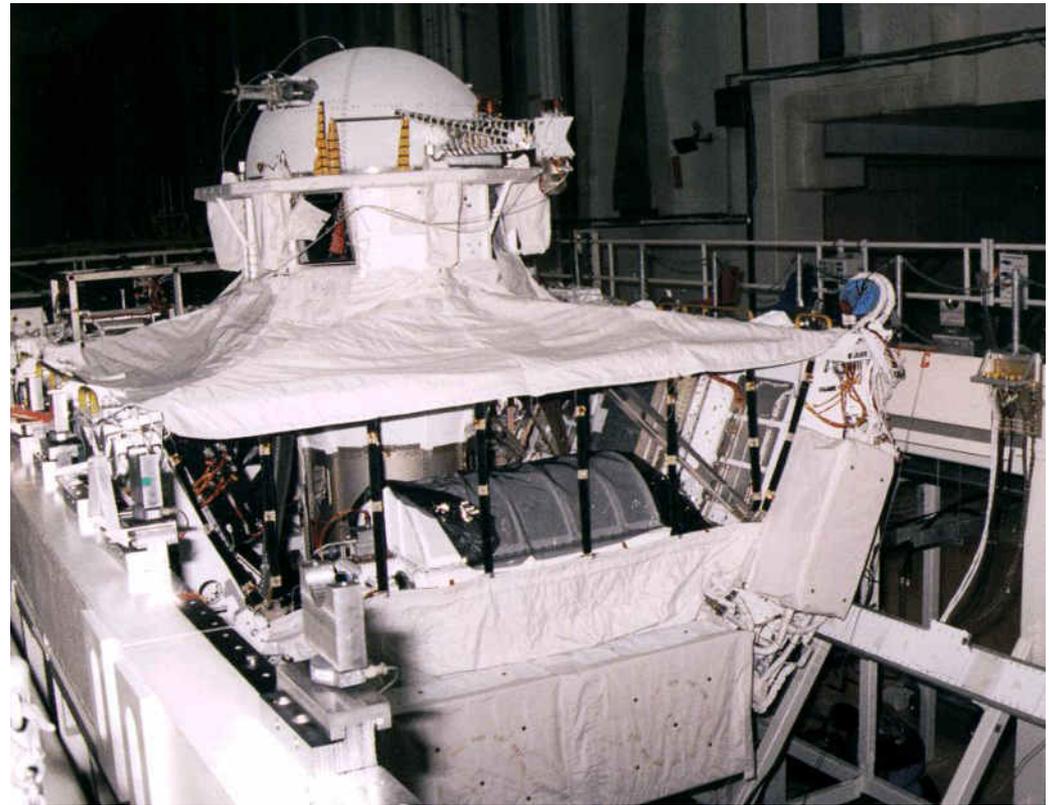


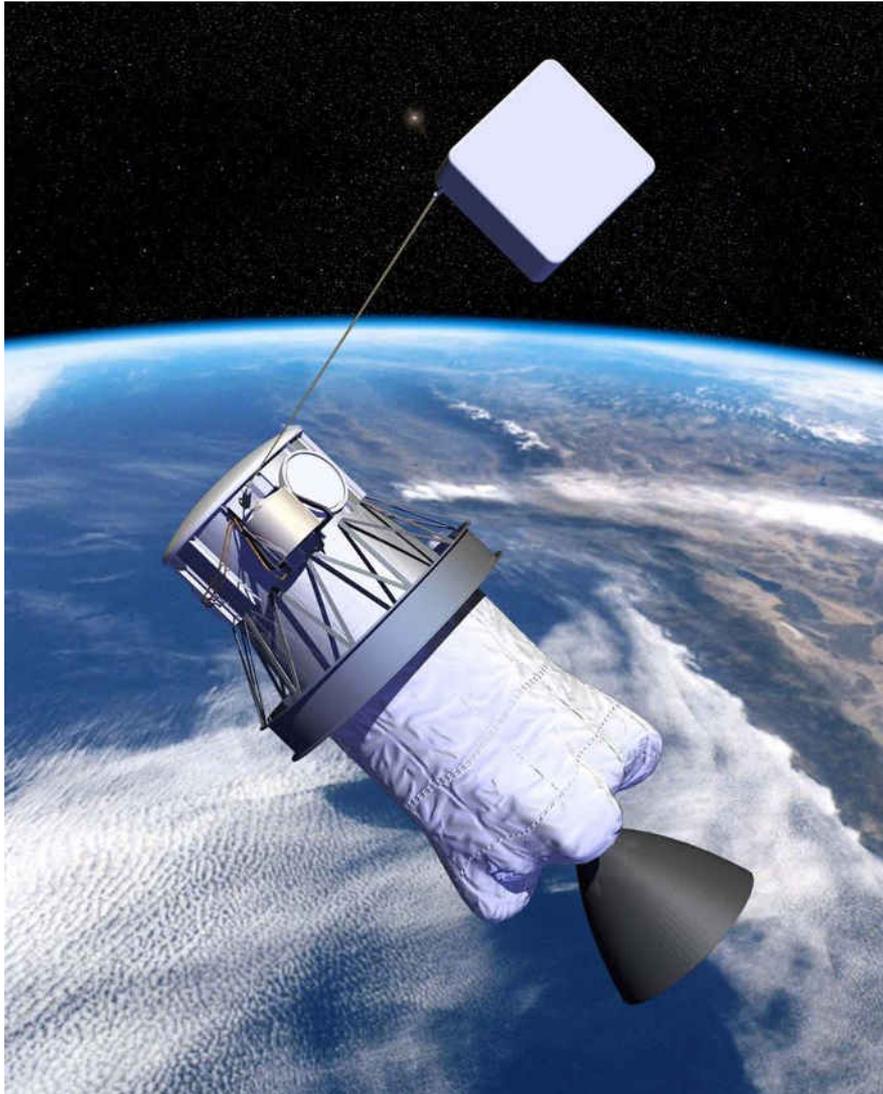
## What did we want to do?

1. Model a tether deployer with retrievable capability
2. Simple & reliable
3. Compact & light



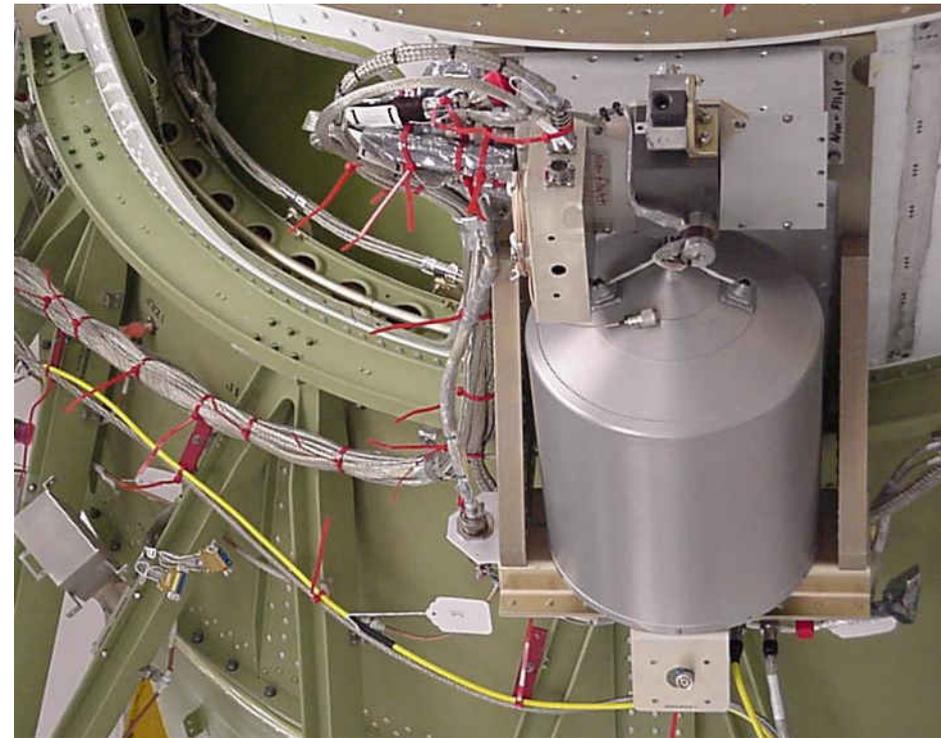
- 1992 – TSS-1 – 20 km tether
- 670 kg satellite + tether
  - 4800 kg pallet & support





1994 – SEDS-II – 20 km tether

- 33 kg tip mass + tether
- 10 kg deployer hardware





# Proposed concept

# Proposed concept (1/2)



# Proposed concept (1/2)



**Deployment  
phase**

# Proposed concept (1/2)



## How to control tether motion during deployment?

*Low-Inertia (SEDS-like)...*

*... Inductive Brake (TSS-like)*



PD control

## How to control tether motion during deployment?

*Low-Inertia (SEDS-like)...*

*... Inductive Brake (TSS-like)*



PD control

## How to control tether motion during deployment?

*Low-Inertia (SEDS-like)...*

*... Inductive Brake (TSS-like)*



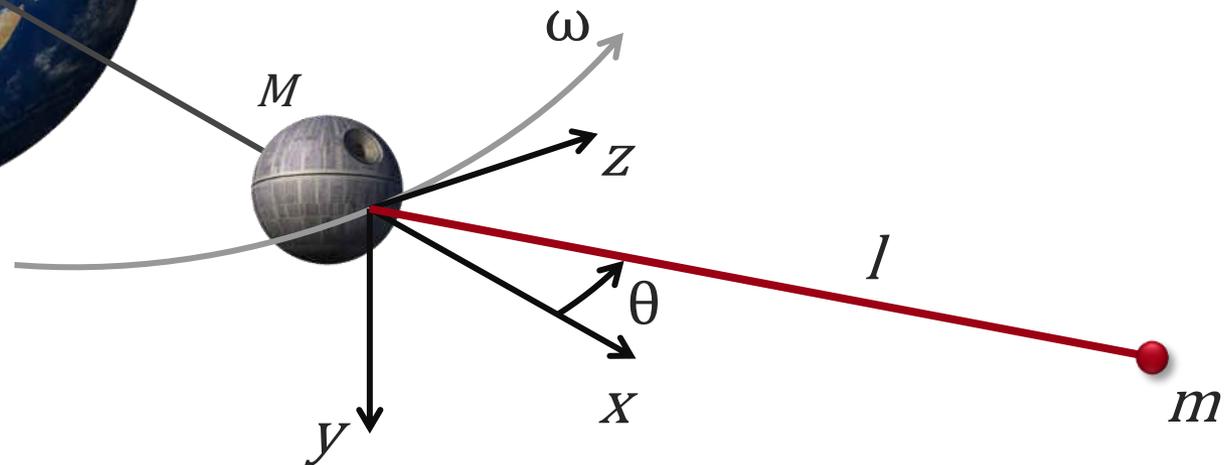
PD control



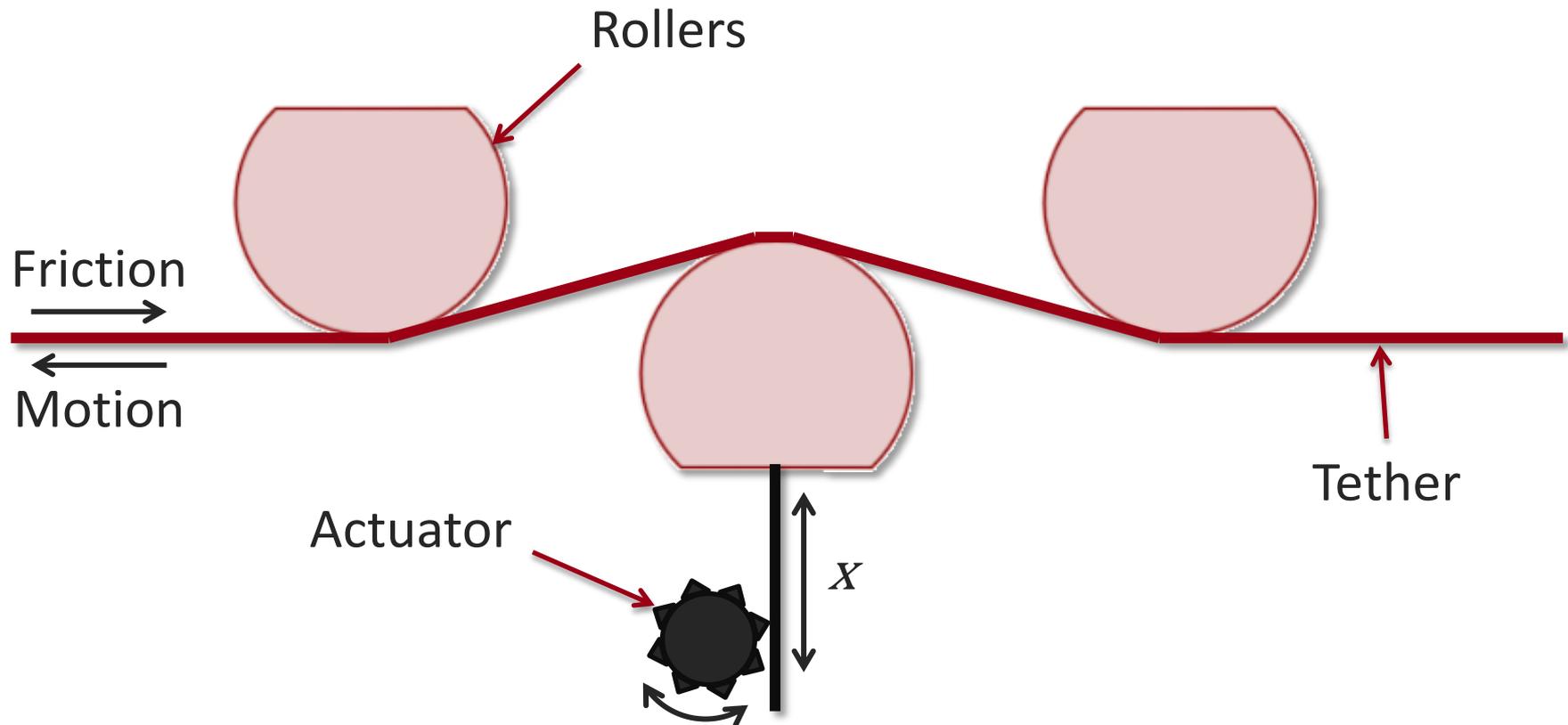
# Models & control



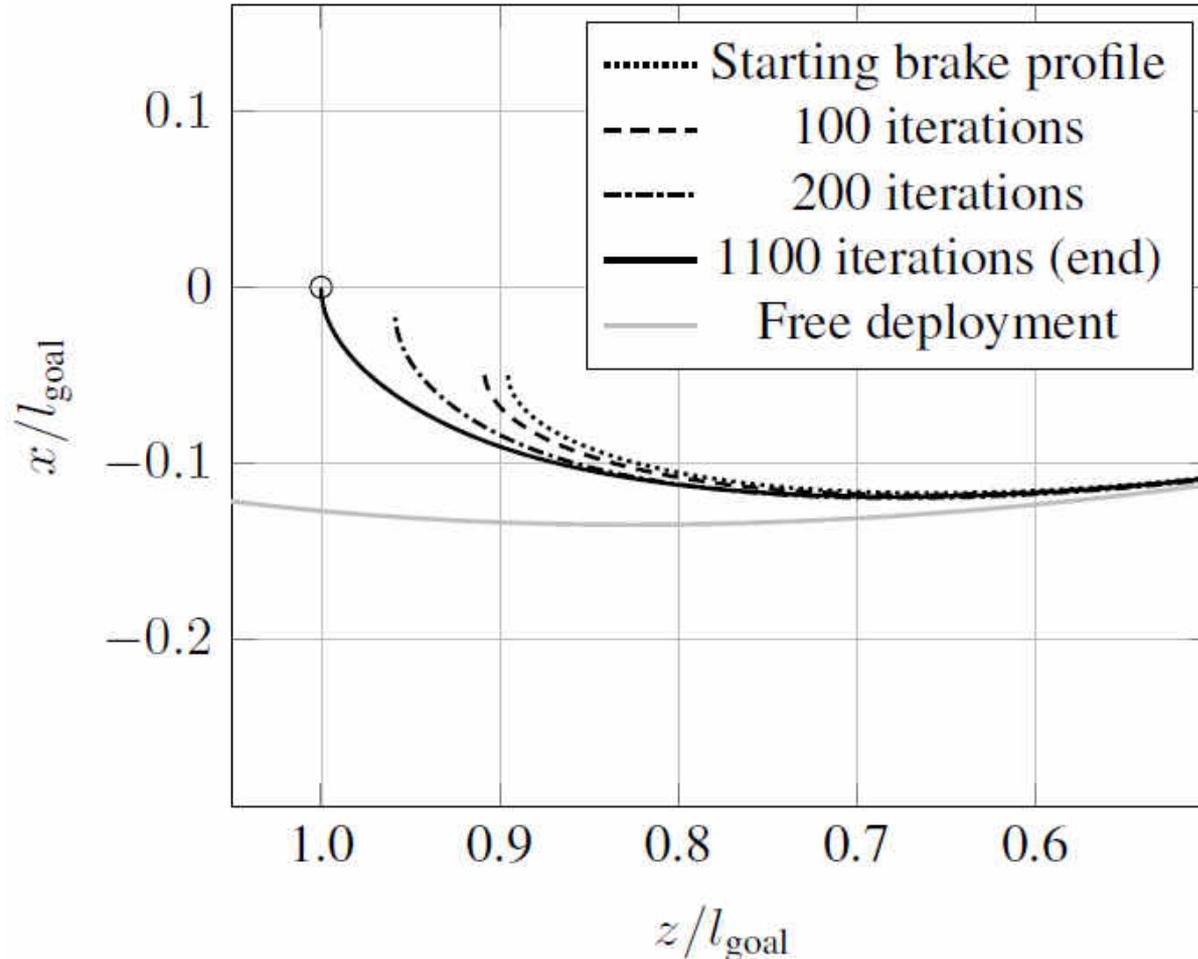
## Dumbbell tether model



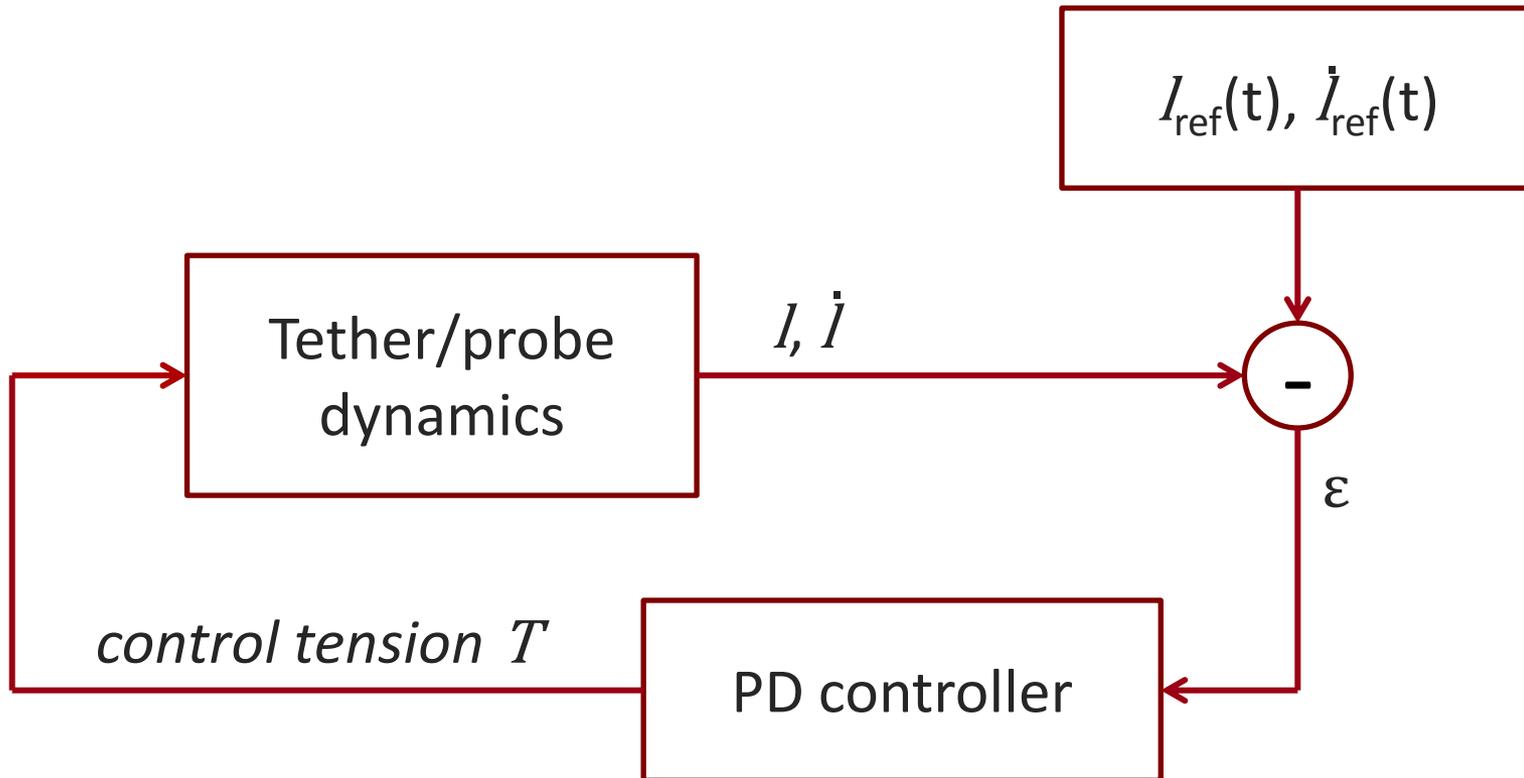
## Mechanical brake (low-inertia)



## Reference trajectory optimization – Nelder-Mead algorithm



Reference trajectories feed-forward –  $l_{\text{ref}}(t), \dot{l}_{\text{ref}}(t)$



$$\text{LI} \left\{ \begin{aligned} \ddot{i}(m + \rho l) + \frac{\rho}{2} \dot{i}^2 + l \left( m + \frac{\rho}{2} l \right) \left[ (\omega + \dot{\theta})^2 + 3\omega \cos^2(\theta) \right] &= -4 \frac{\lambda p}{d} x - T_0 \\ \ddot{\theta} + 3 \frac{2m + \rho l}{3m + \rho l} (\omega + \dot{\theta}) \frac{\dot{l}}{l} + 3\omega^2 \sin(\theta) \cos(\theta) &= 0 \end{aligned} \right.$$

$$\text{IB} \left\{ \begin{aligned} J \frac{\partial i}{\partial t} + Ri &= V - k_v \dot{\psi} \\ \ddot{\psi} \left[ \frac{I}{r} + r(m + \rho r \psi) \right] + \dot{\psi} \left( \frac{b}{r} + \frac{\rho}{2} r^2 \dot{\psi} \right) - \psi r \left( m + \frac{\rho}{2} r \psi \right) \left[ (\omega + \dot{\theta})^2 + \dots \right. \\ &\quad \left. \dots + 3\omega^2 \cos^2(\theta) \right] = -\frac{k_t}{r} i - T_0 \\ \ddot{\theta} + 3 \frac{2m + \rho \psi r}{3m + \rho \psi r} (\omega + \dot{\theta}) \frac{\dot{\psi}}{\psi} + 3\omega^2 \sin(\theta) \cos(\theta) &= 0 \end{aligned} \right.$$

# Equations (deployment)



LI

$$\begin{cases} \ddot{l}(m + \rho l) + \frac{\rho}{2}\dot{l}^2 + l\left(m + \frac{\rho}{2}l\right) \left[ (\omega + \dot{\theta})^2 + 3\omega \cos^2(\theta) \right] = -4\frac{\lambda p}{d}x - T_0 \\ \ddot{\theta} + 3\frac{2m + \rho l}{3m + \rho l} (\omega + \dot{\theta}) \frac{\dot{l}}{l} + 3\omega^2 \sin(\theta) \cos(\theta) = 0 \end{cases}$$

IB

$$\begin{cases} J\frac{\partial i}{\partial t} + Ri = V - k_v\dot{\psi} \\ \ddot{\psi} \left[ \frac{I}{r} + r(m + \rho r\psi) \right] + \dot{\psi} \left( \frac{b}{r} + \frac{\rho}{2}r^2\dot{\psi} \right) - \psi r \left( m + \frac{\rho}{2}r\psi \right) \left[ (\omega + \dot{\theta})^2 + \dots \right. \\ \left. \dots + 3\omega^2 \cos^2(\theta) \right] = -\frac{k_t}{r}i - T_0 \\ \ddot{\theta} + 3\frac{2m + \rho\psi r}{3m + \rho\psi r} (\omega + \dot{\theta}) \frac{\dot{\psi}}{\psi} + 3\omega^2 \sin(\theta) \cos(\theta) = 0 \end{cases}$$

Control

Inner friction

# Equations (deployment)

LI

$$\left\{ \begin{aligned} \ddot{l}(m + \rho l) + \frac{\rho}{2}\dot{l}^2 + l\left(m + \frac{\rho}{2}l\right) \left[ (\omega + \dot{\theta})^2 + 3\omega \cos^2(\theta) \right] &= -4\frac{\lambda p}{d}x - T_0 \\ \ddot{\theta} + 3\frac{2m + \rho l}{3m + \rho l} (\omega + \dot{\theta}) \frac{\dot{l}}{l} + 3\omega^2 \sin(\theta) \cos(\theta) &= 0 \end{aligned} \right.$$

IB

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Control

Inner friction

15 mN

150 mN

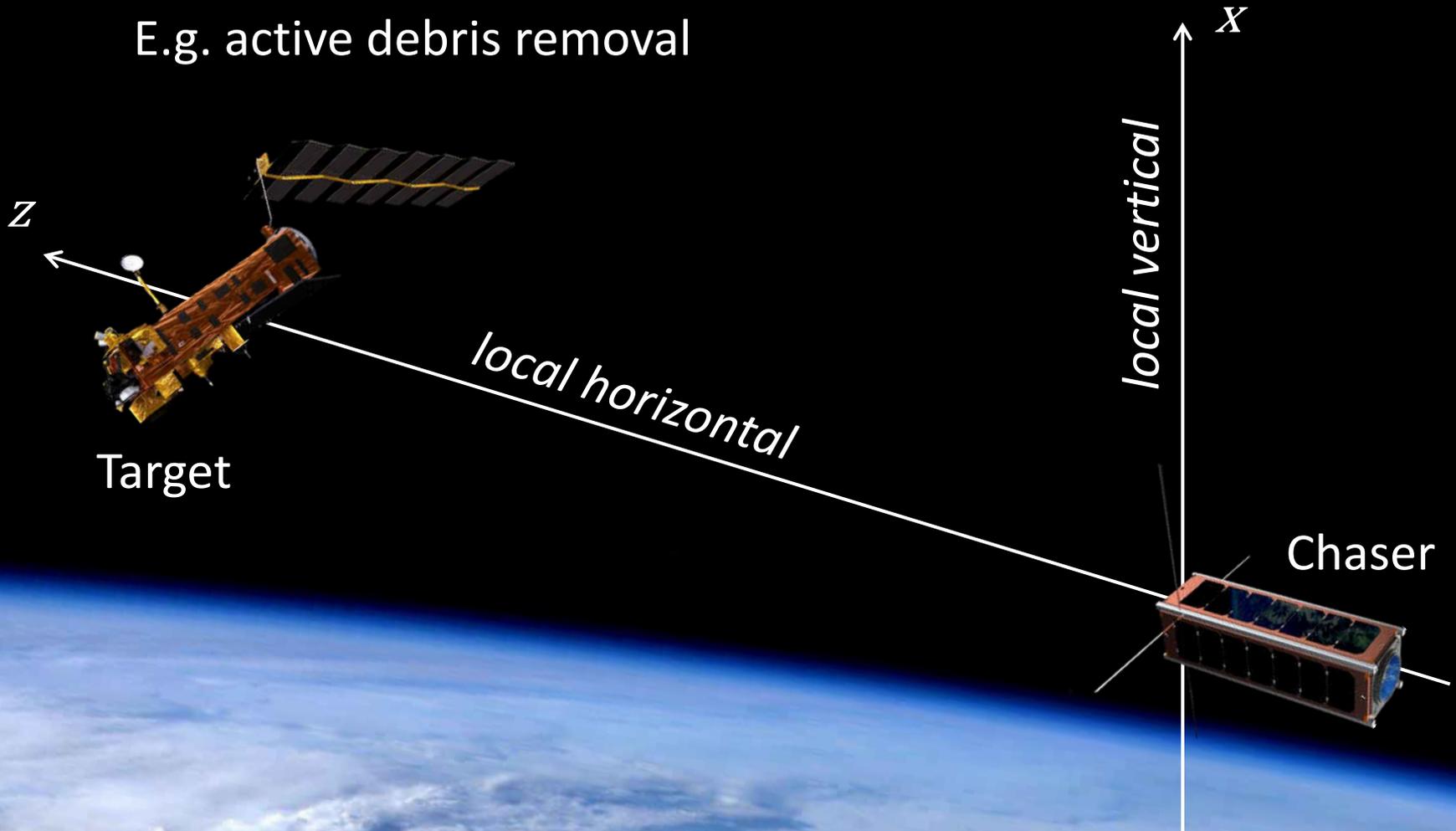


# Simulations

# Deployment scenario (1/2)



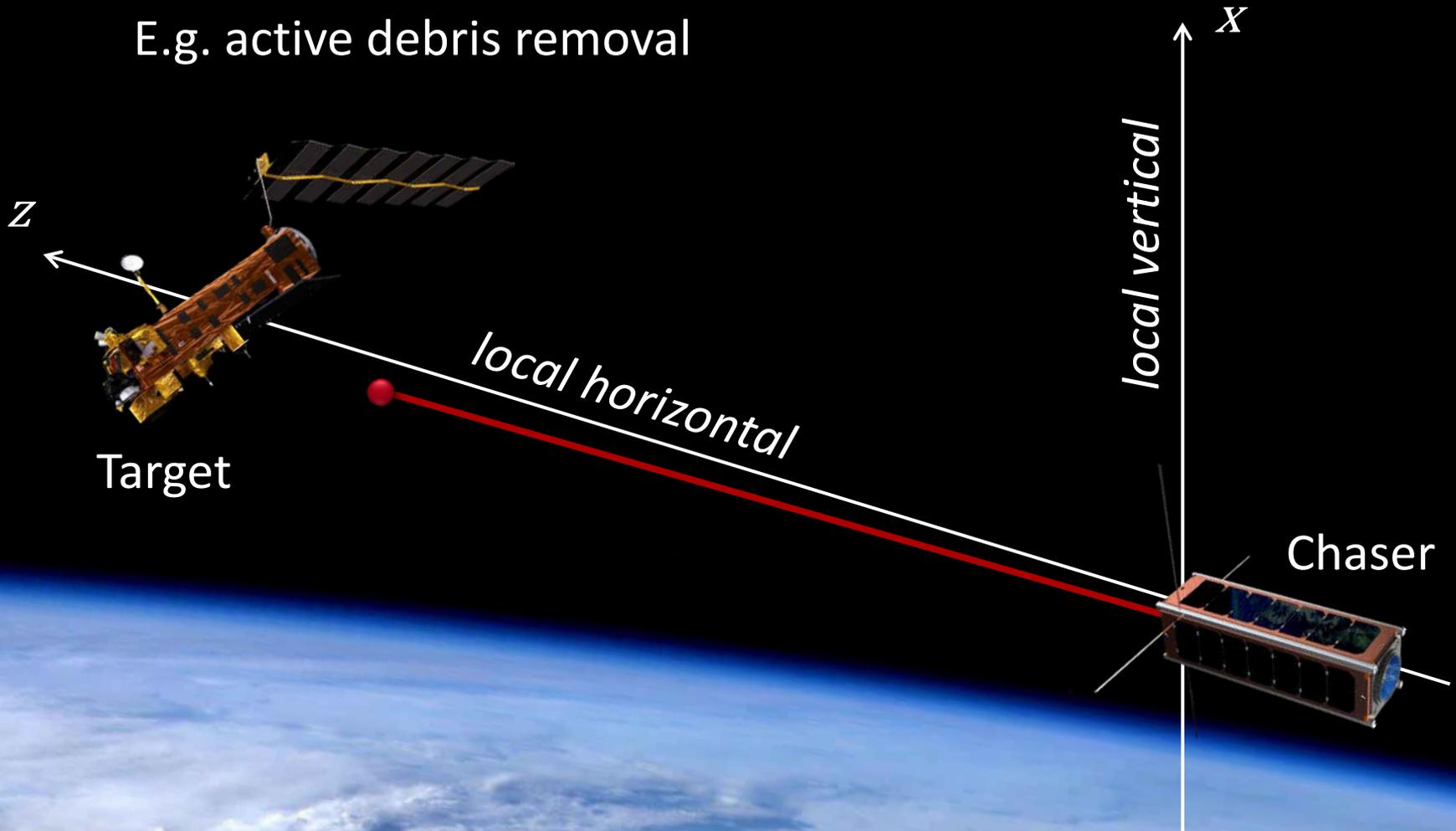
E.g. active debris removal



# Deployment scenario (1/2)



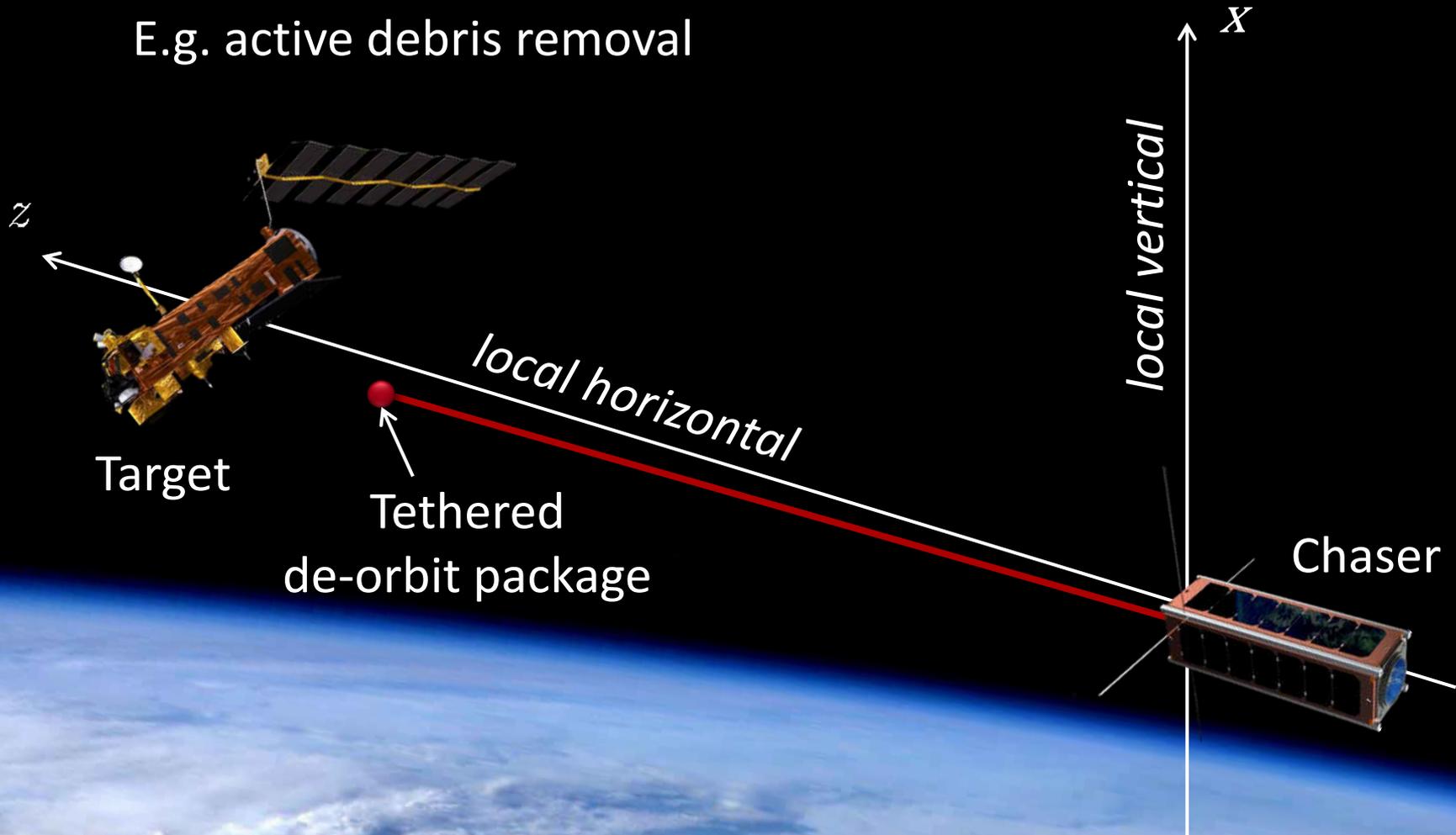
E.g. active debris removal

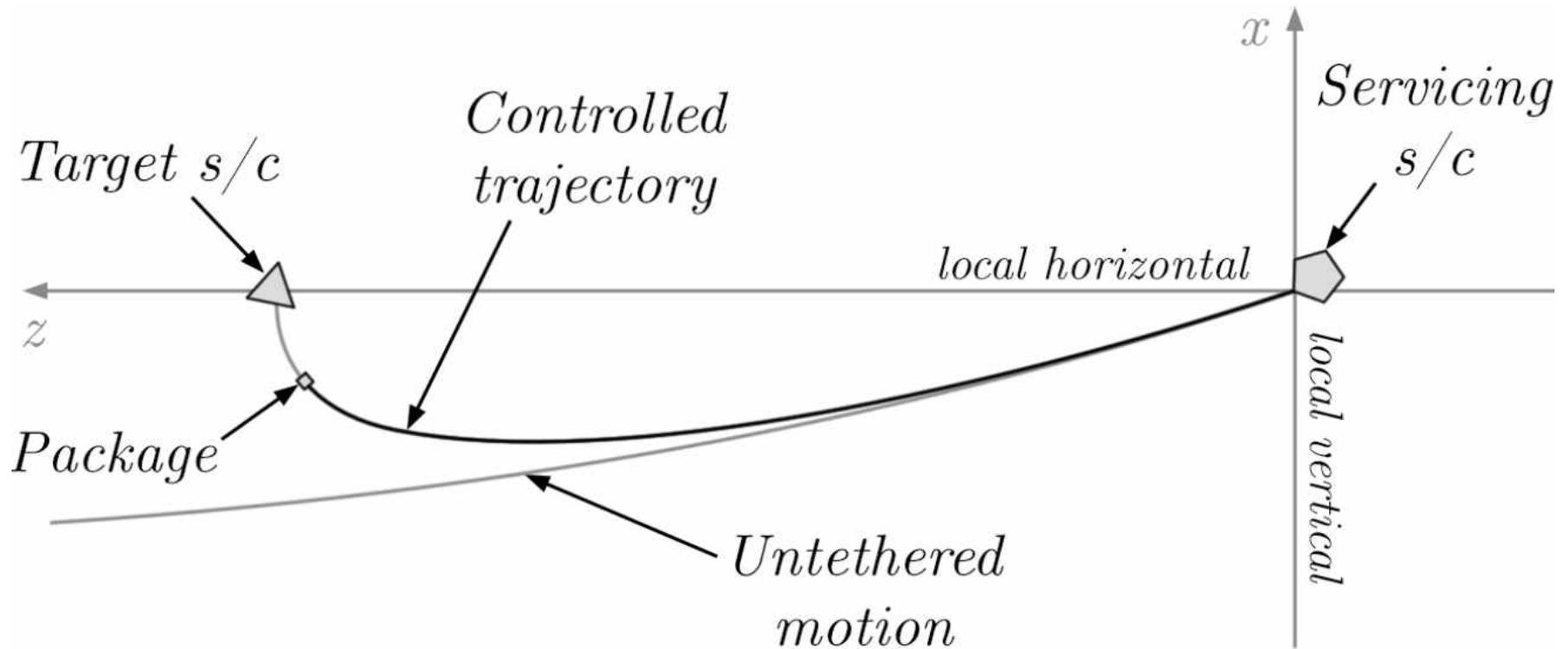


# Deployment scenario (1/2)

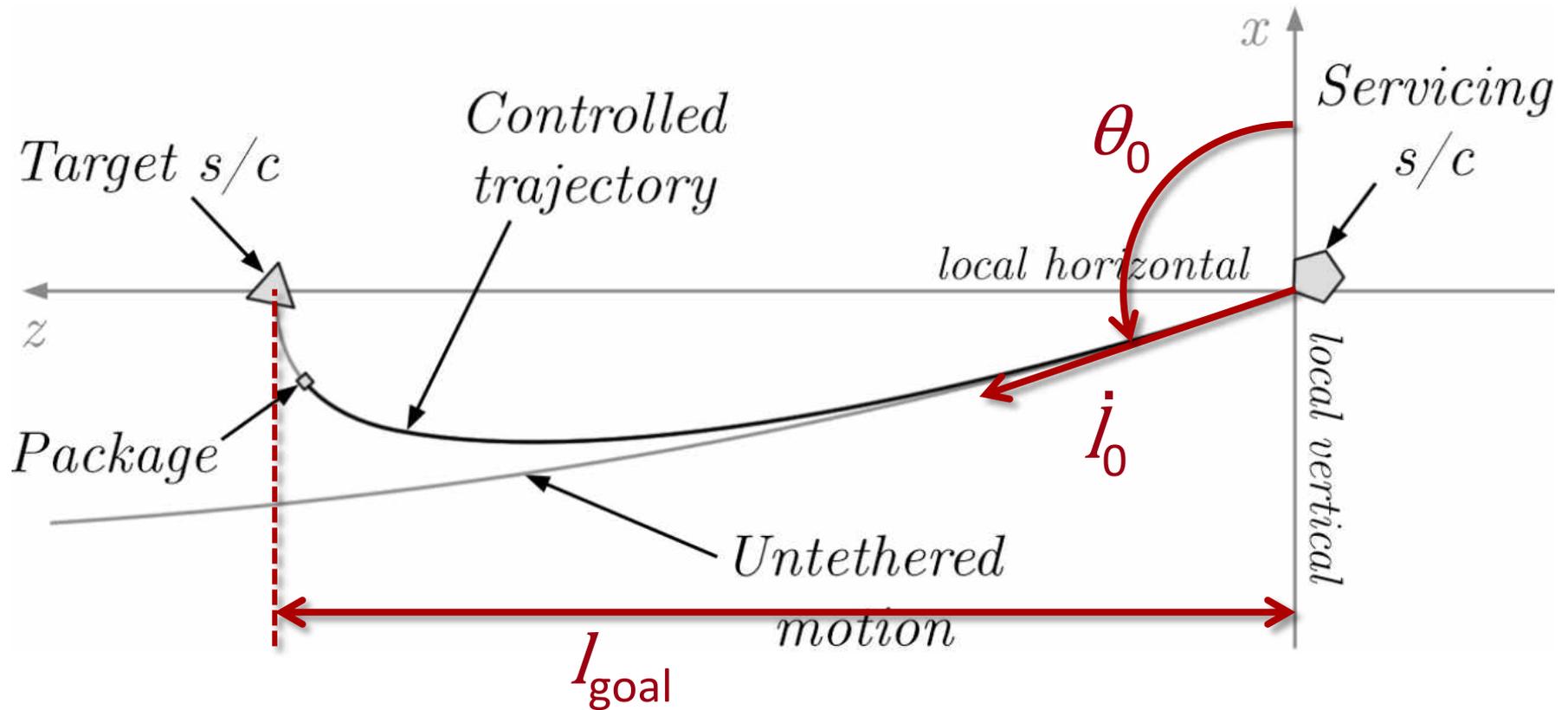


E.g. active debris removal





# Deployment scenario (2/2)



## Simulations results

$l_{\text{goal}}$ (m) $\rightarrow$	50		100		200	
$\dot{l}_0$ (m/s) $\downarrow$	LI	IB	LI	IB	LI	IB
0.50	●	⊖	●	⊖	⊖	⊖
0.75	⊕	⊖	●	⊖	●	⊖
1.00	⊕	●	⊕	⊖	●	⊖
1.50	⊕	●	⊕	●	⊕	⊖
1.75	⊕	●	⊕	●	⊕	⊖
2.00	⊕	●	⊕	●	⊕	●

(●): successful deployments

(⊕): insufficient brake authority control

(⊖): insufficient initial velocity

## Simulations results

$l_{\text{goal}}$ (m) $\rightarrow$	50		100		200	
$\dot{l}_0$ (m/s) $\downarrow$	LI	IB	LI	IB	LI	IB
0.50	●	⊖	●	⊖	⊖	⊖
0.75	⊕	⊖	●	⊖	●	⊖
1.00	⊕	●	⊕	⊖	●	⊖
1.50	⊕	●	⊕	●	⊕	⊖
1.75	⊕	●	⊕	●	⊕	⊖
2.00	⊕	●	⊕	●	⊕	●

Required higher  
launch velocity

(●): successful deployments

(⊕): insufficient brake authority control

(⊖): insufficient initial velocity

## Simulations results

$l_{\text{goal}}$ (m) $\rightarrow$	50		100		200	
$\dot{l}_0$ (m/s) $\downarrow$	LI	IB	LI	IB	LI	IB
0.50	●	⊖	●	⊖	⊖	⊖
0.75	⊕	⊖	●	⊖	●	⊖
1.00	⊕	●	⊕	⊖	●	⊖
1.50	⊕	●	⊕	●	⊕	⊖
1.75	⊕	●	⊕	●	⊕	⊖
2.00	⊕	●	⊕	●	⊕	●

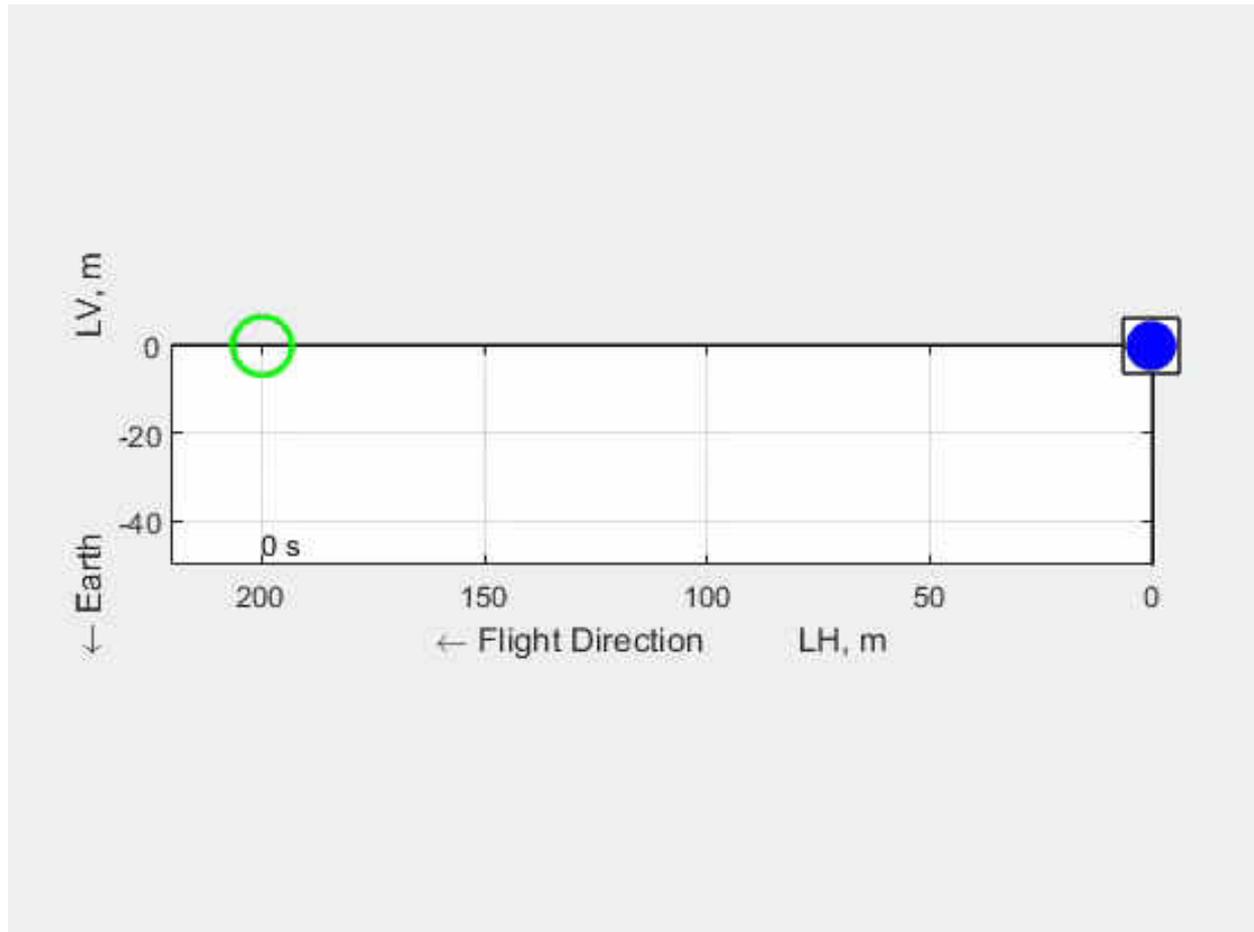
Less control authority  
w.r.t. IB

(●): successful deployments

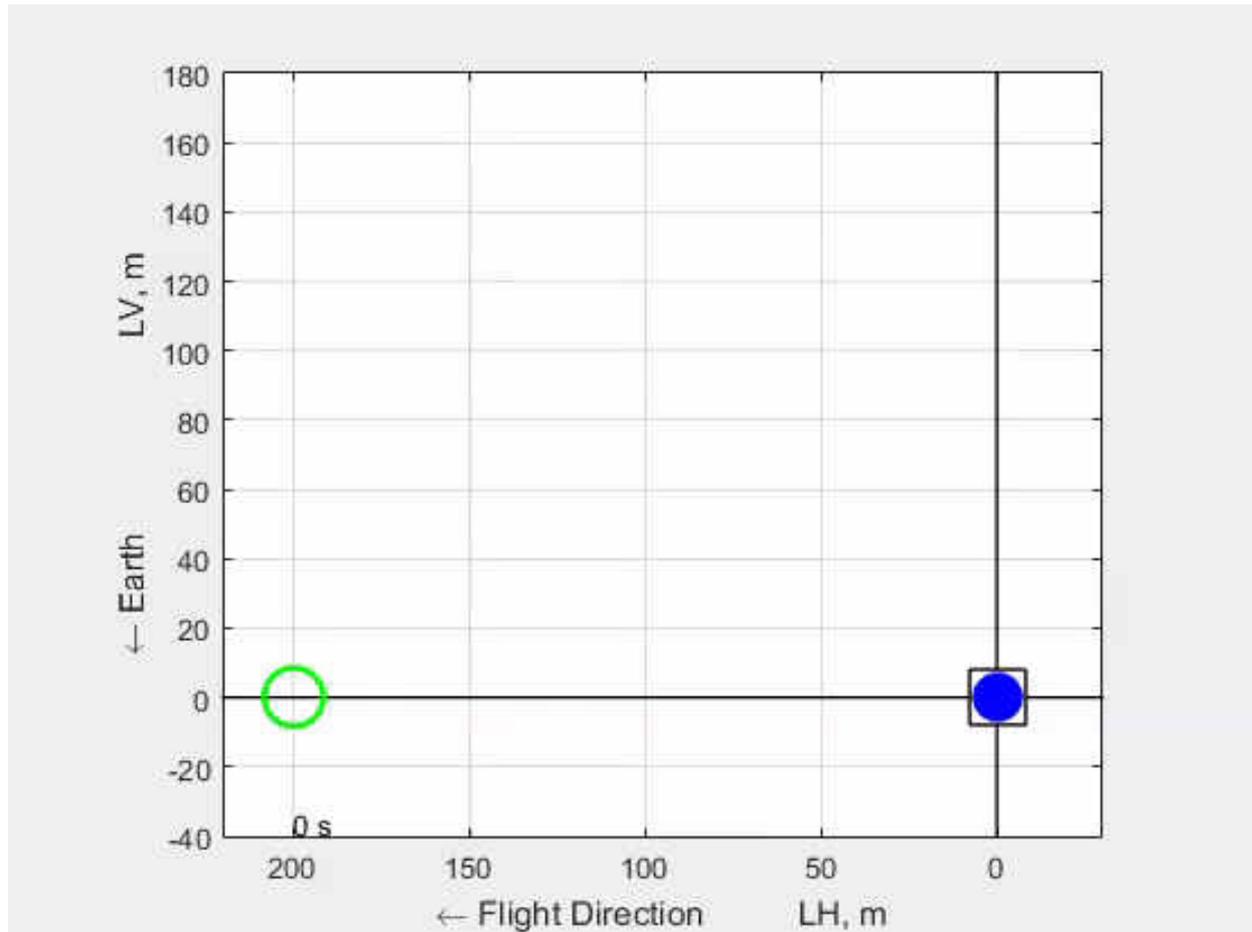
(⊕): insufficient brake authority control

(⊖): insufficient initial velocity

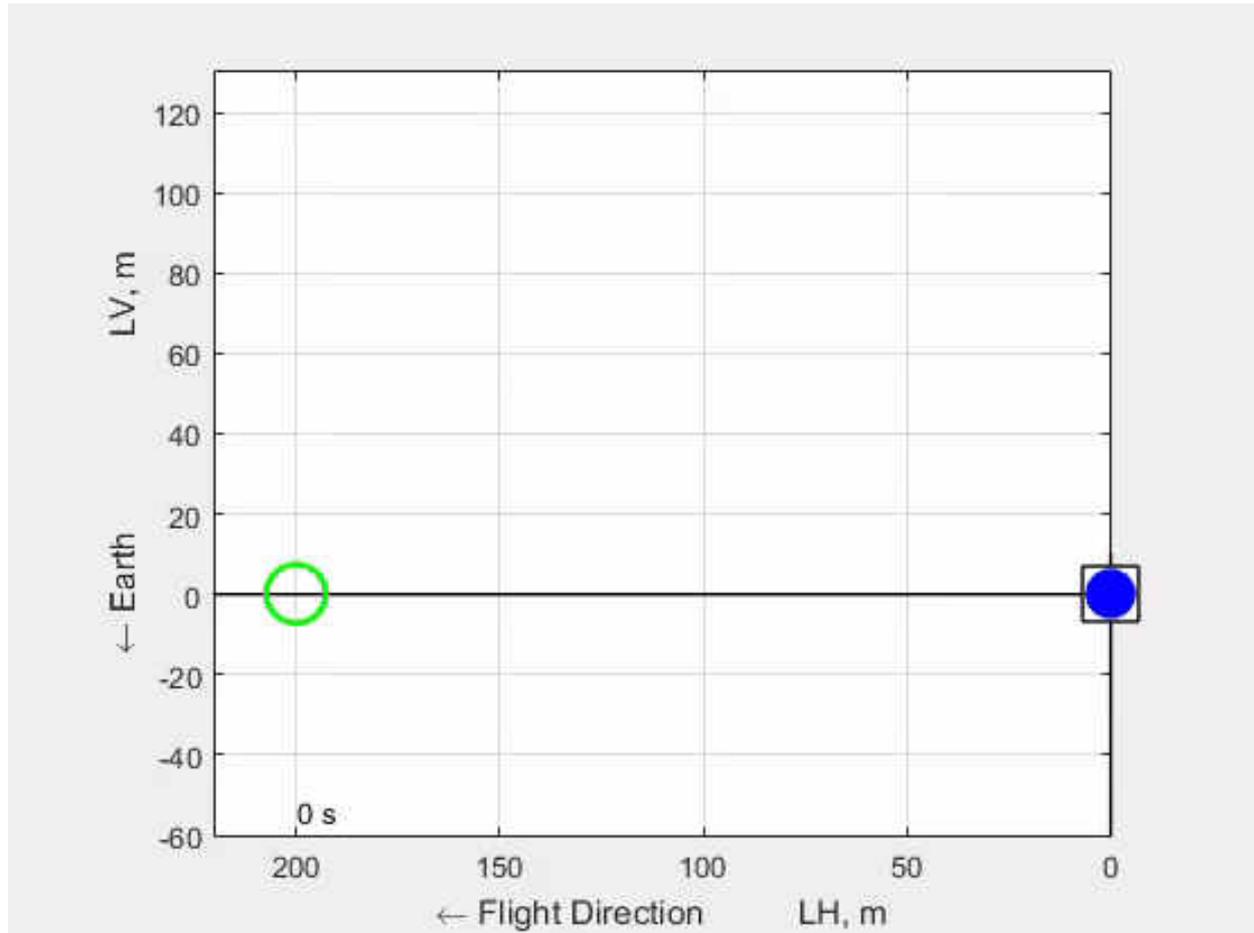
## Successful deployment



## Deployment failure – insufficient launch velocity



## Deployment failure – insufficient deployer control authority





# Conclusions

## *Inductive brake*

1. More control authority
2. Less actuators
3. Some critical issues during deployment are addressed

## *Low-inertia*

1. Easier ground test phase
2. Requires less energy ( $T_0$ )
3. Higher tolerance of design inaccuracies (less parts in synch. motion)

## *Inductive brake*

1. More control authority
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## *Low-inertia*

1. Easier ground test phase
2. Requires less energy ( $T_0$ )
3. Higher tolerance of design inaccuracies (less parts in synch. motion)



- Questions? -





## 2007 – YES2

- 12 kg endmass + tether
- 24 kg deployment hardware



$$\ddot{l} = -\frac{\rho \dot{l}^2}{2(m + \rho l)} + l \frac{2m + \rho l}{2(m + \rho l)} \left[ (\omega + \dot{\theta})^2 + 3\omega^2 \cos^2(\theta) \right] - \frac{T}{m + \rho l}$$

$$\ddot{\theta} = -3 \frac{2m + \rho l}{3m + \rho l} (\omega + \dot{\theta}) \frac{\dot{l}}{l} - 3\omega^2 \sin(\theta) \cos(\theta)$$

# Extras – motion equations



Convective

Gravity gradient

Tether tension (control)

Centrifugal

$$\ddot{l} = \frac{\rho \dot{l}^2}{2(m + \rho l)} + l \frac{2m + \rho l}{2(m + \rho l)} \left[ (\omega + \dot{\theta})^2 + 3\omega^2 \cos^2(\theta) \right] - \frac{T}{m + \rho l}$$

$$\ddot{\theta} = -3 \frac{2m + \rho l}{3m + \rho l} (\omega + \dot{\theta}) \frac{\dot{l}}{l} - 3\omega^2 \sin(\theta) \cos(\theta)$$

Stabilizing if  $\dot{l} > 0$

Parameter	Value	Unit
$b$	$3 \cdot 10^{-6}$	Ns/rad
$d$	$9 \cdot 10^{-2}$	m
$e$	0	1
$I$	$17 \cdot 10^{-7}$	kg m <sup>2</sup>
$J$	$3.65 \cdot 10^{-4}$	H
$k_v$	$4.05 \cdot 10^{-3}$	Vs/rad
$k_t$	$3.8675 \cdot 10^{-2}$	Nm/A
$p$	$3 \cdot 10^{-2}$	m
$r$	$15 \cdot 10^{-2}$	m
$R$	2.98	$\Omega$
$T_{0,li}$	$15 \cdot 10^{-3}$	N
$T_{0,ib}$	$150 \cdot 10^{-3}$	N
$m$	20	kg
$\lambda$	0.5	N/m
$\rho$	$1.35 \cdot 10^{-3}$	kg/m
$\omega$	$1.0382 \cdot 10^{-3}$	rad/s

Low-inertia

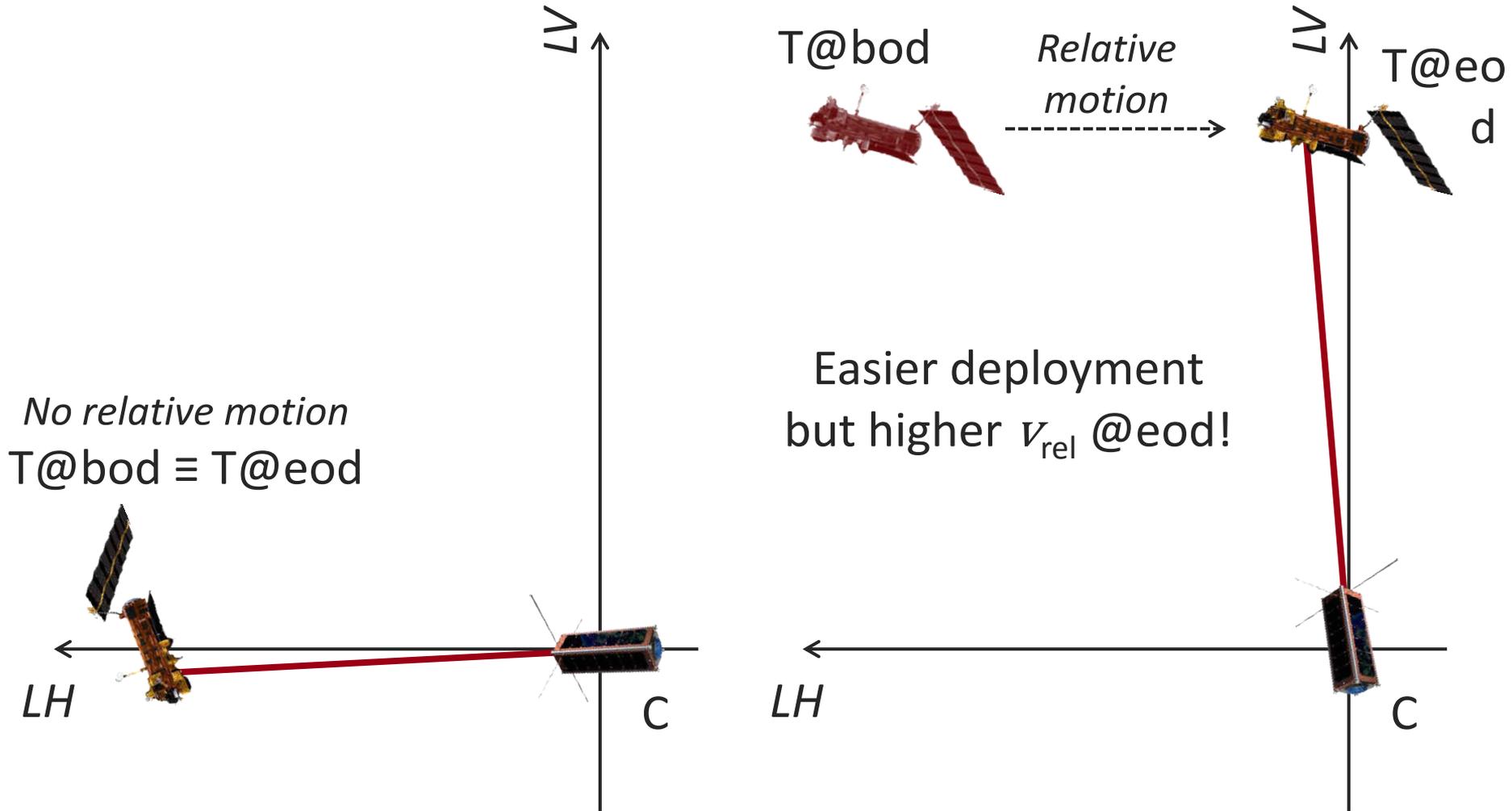


Inductive brake



Higher inner friction in IB due to more sliding parts

# Extras – deployment scenario



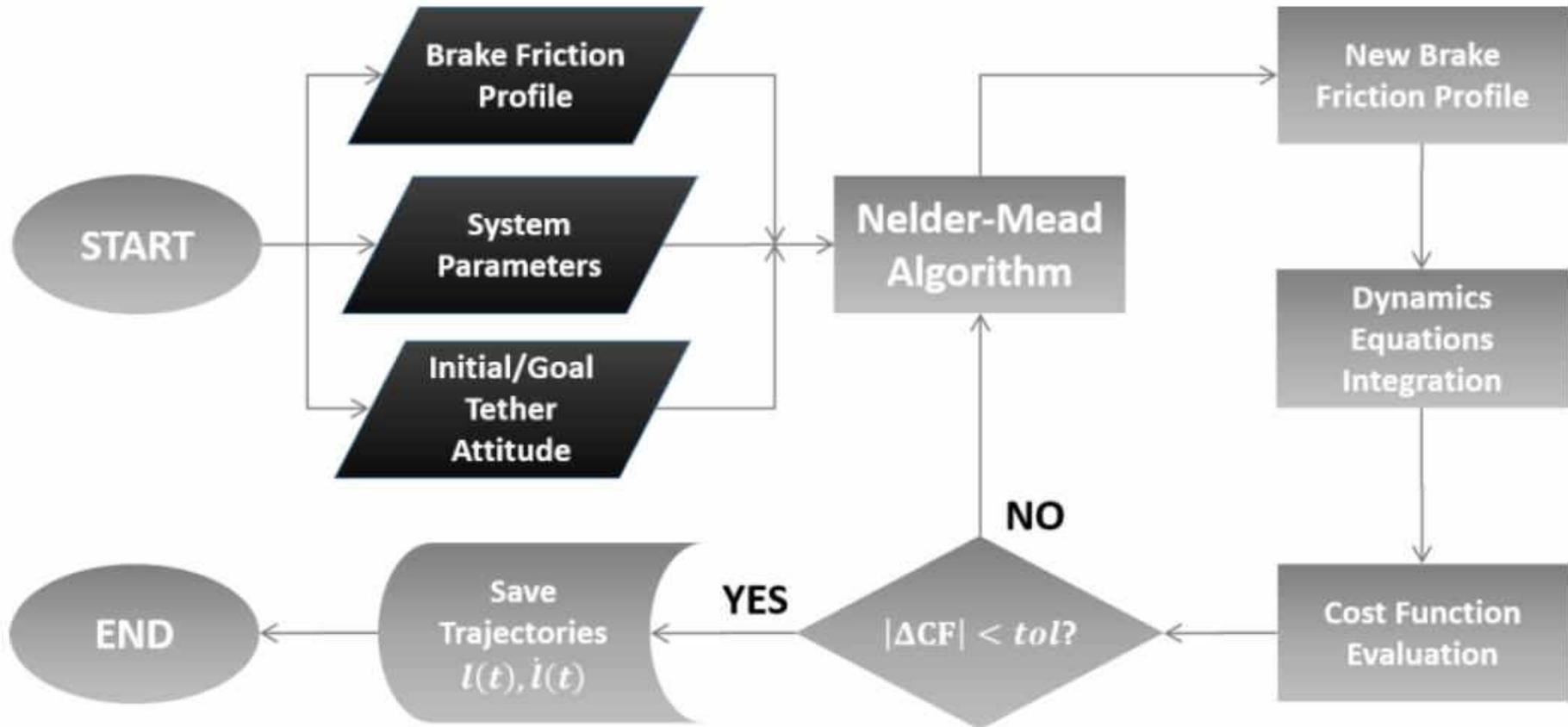
$\theta_0$  values chosen in the simulations

$l_{\text{goal}}$ (m) $\rightarrow$	50	100	200
$\dot{l}_0$ (m/s) $\downarrow$			
0.50	103°	115°	134°
0.75	99°	107°	123°
1.00	96°	101°	114°
1.50	95°	98°	108°
1.75	94.5°	97°	105°
2.00	94°	96°	102°

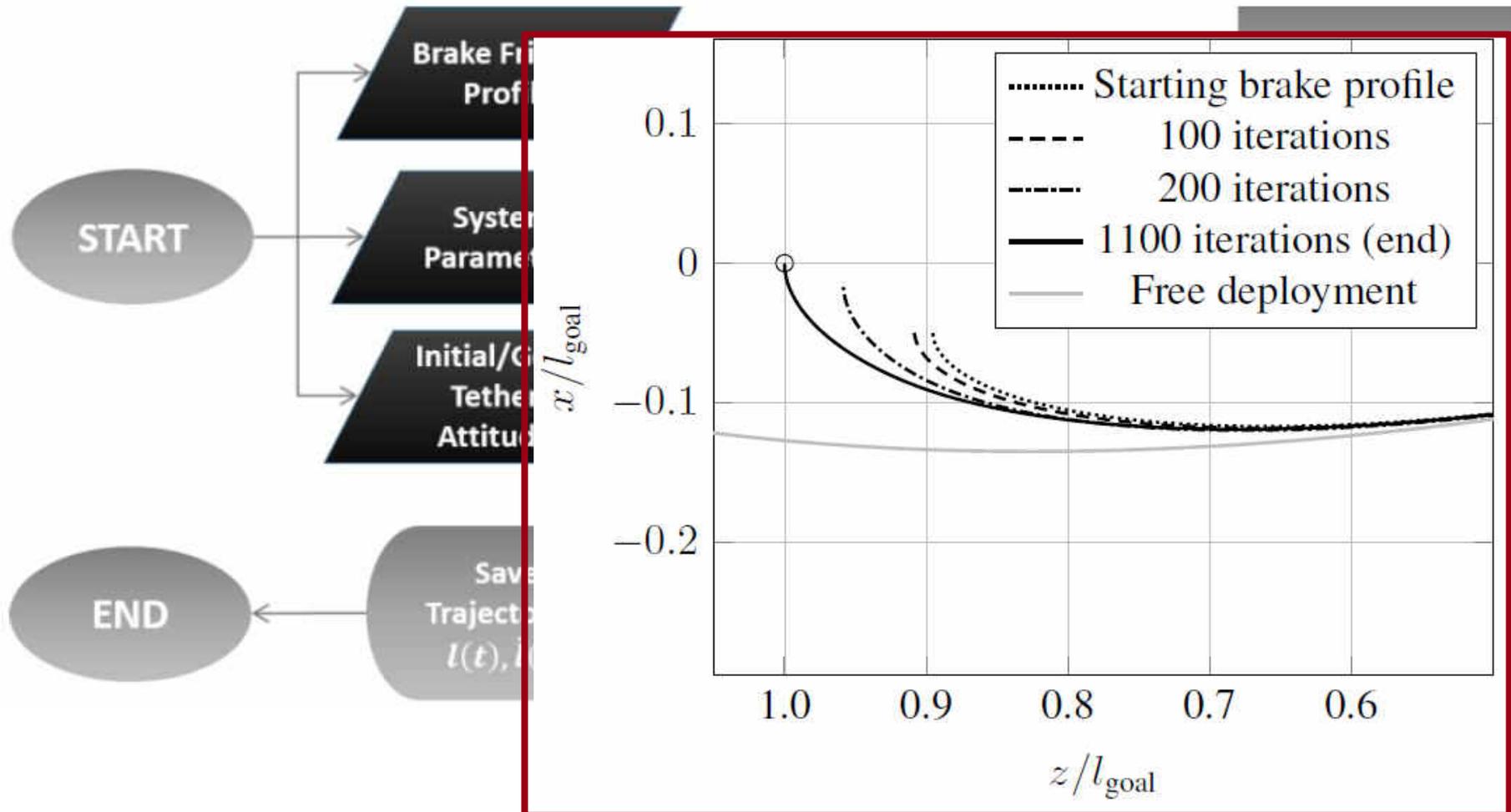
$$\theta_0 = \theta_{\text{goal}} - \bar{\dot{\theta}} t_{\text{end}}$$

$\bar{\dot{\theta}} = \bar{\dot{\theta}}(\omega, \theta_{\text{goal}}, l_{\text{goal}}, \dot{l}_0)$   
 $t_{\text{end}} = t_{\text{end}}(\dot{l}_0, T_0, \bar{F}_{\text{friction}})$

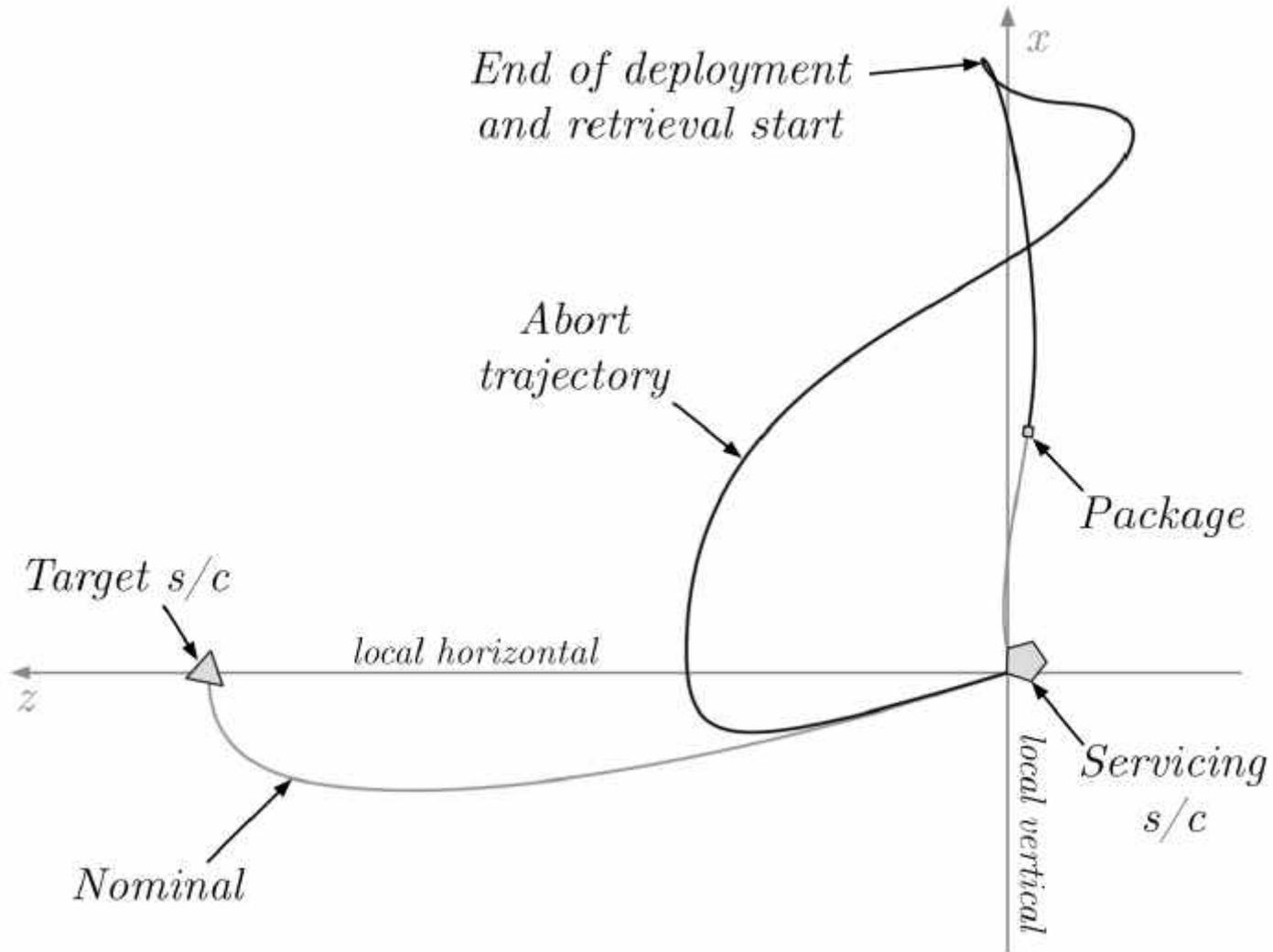
# Extras – Nelder-Mead algorithm



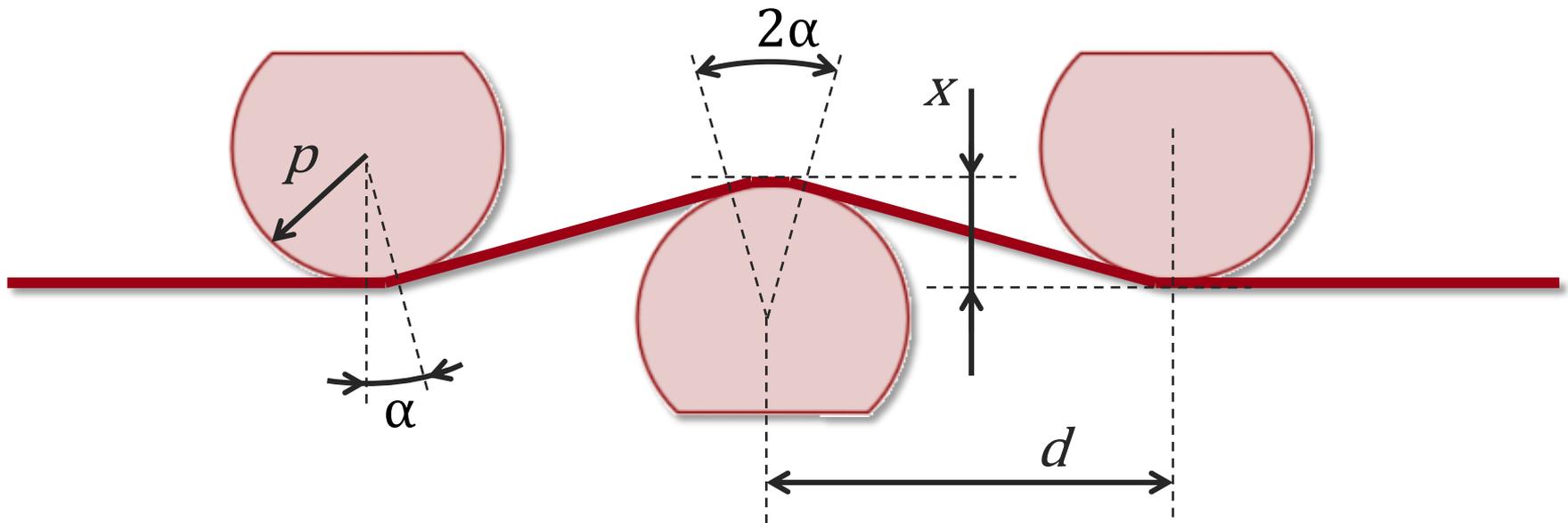
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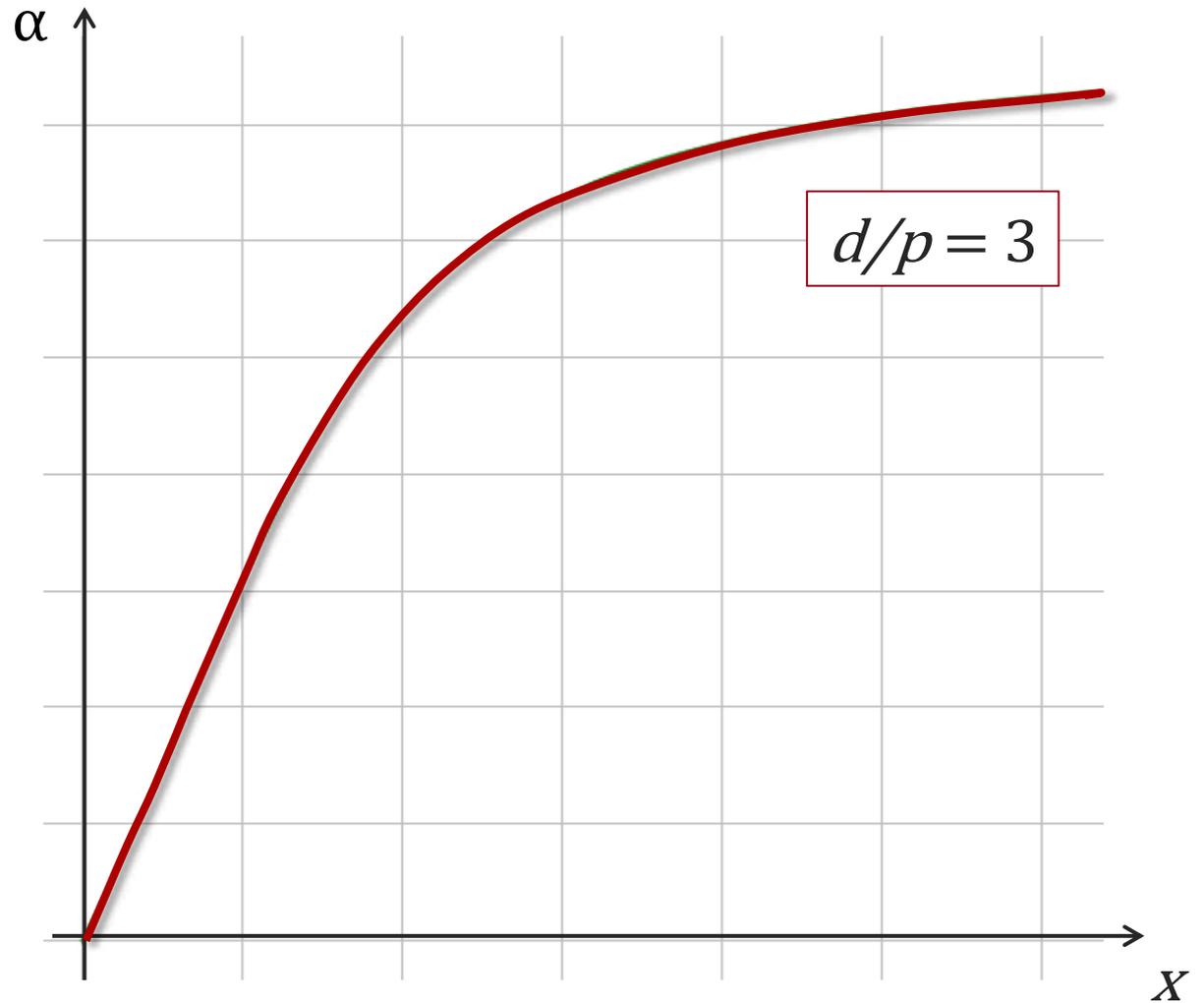
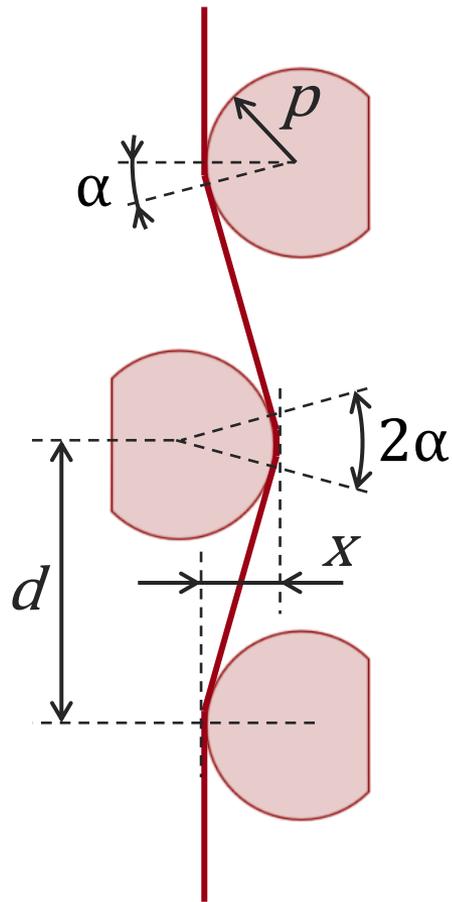


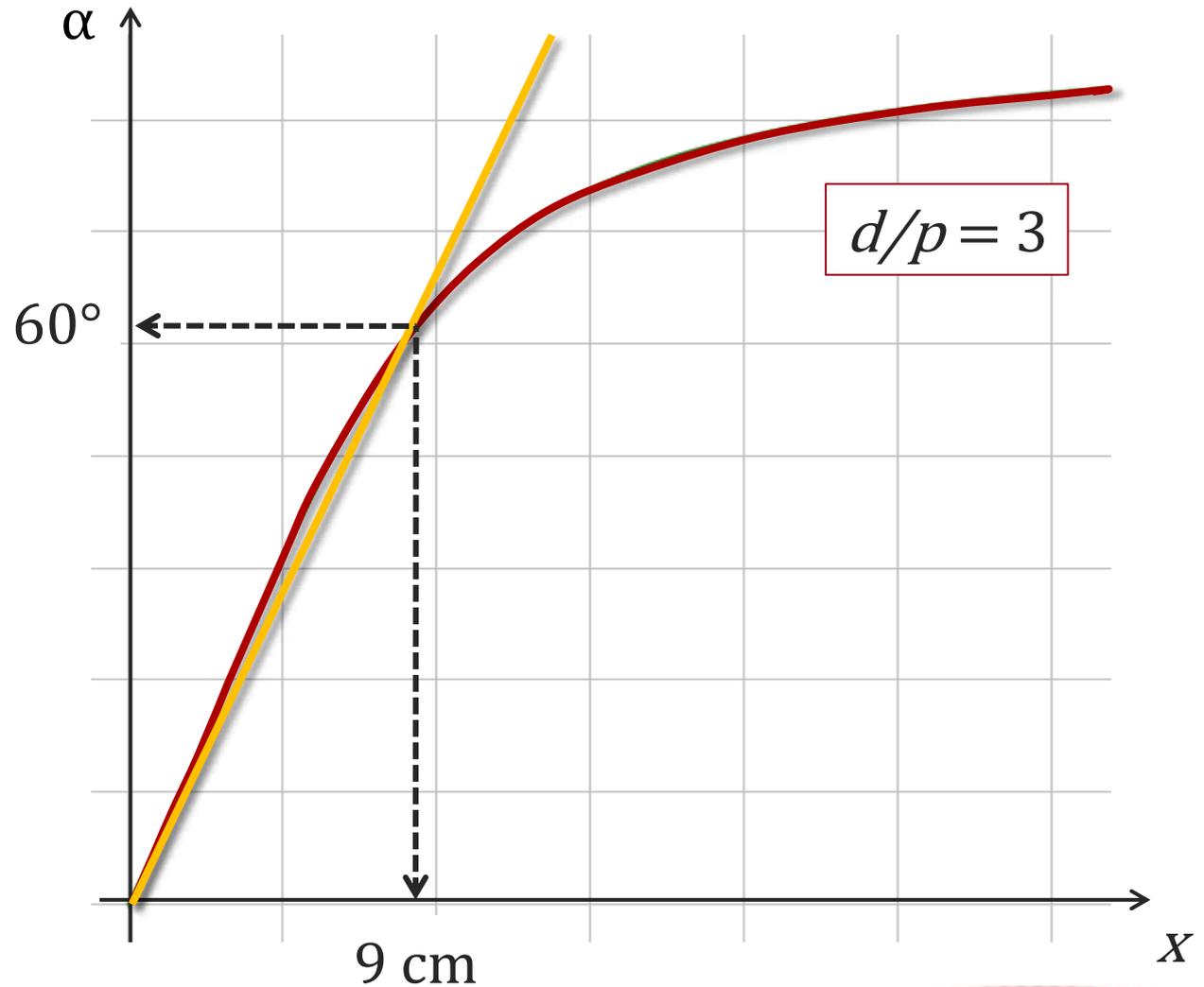
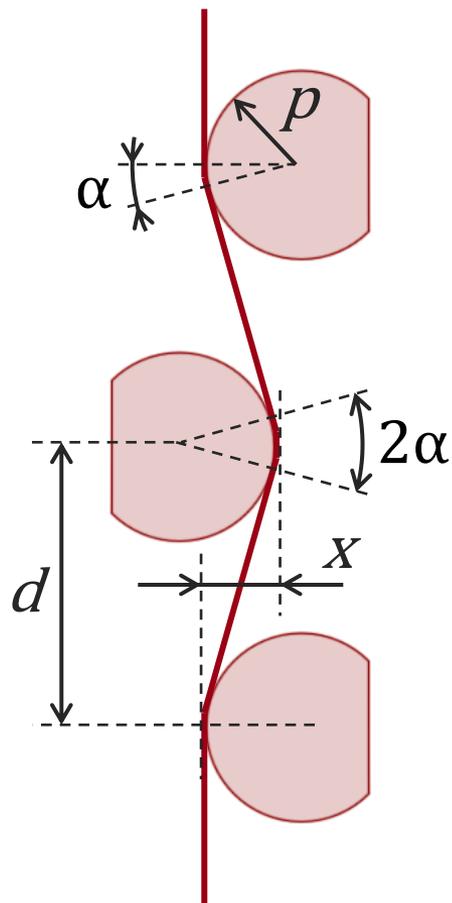
# Extras – abort capability



## Mechanical brake







## What could we do? New docking techniques

